



**Workshop “Galileo Galilei” (GG) and GGG lab prototype:
state of the art and new possibilities”**



GG error budget from the end-to-end simulator developed at TAS-I



ISTITUTO
NAZIONALE
DI RICERCA
METROLOGICA



Giuseppe Catastini
ThalesAlenia Space Italia, Torino

THALES

BL OOS

12.02.2010

GG workshop, Pisa / S.Piero a Grado

**INTERNAL THALES ALENIA SPACE
COMMERCIAL IN CONFIDENCE**

All rights reserved, 2010, Thales Alenia Space

The Signal

- Scientific objective: $\eta = 10^{-17}$
- Signal optimization: choice of the test masses materials
- Signal optimization: choice of the orbit

- TMs differential acceleration due to EP violation:

$$a_{EP} = g(h) \cdot 10^{-17} \text{ m/s}^2$$



- Orbit altitude h as low as possible to maximise $g(h)$, but h as high as possible to match air drag reference acceleration (depending on s/c A/M and solar activity during flight) $a_{NG_{xy}}^{ext} \approx 2 \times 10^{-7} \text{ m/s}^2$

- GG Phase A2 study spacecraft final configuration:

- $m_{s/c} = 346.21 \text{ kg}$ (launch mass, no margin)

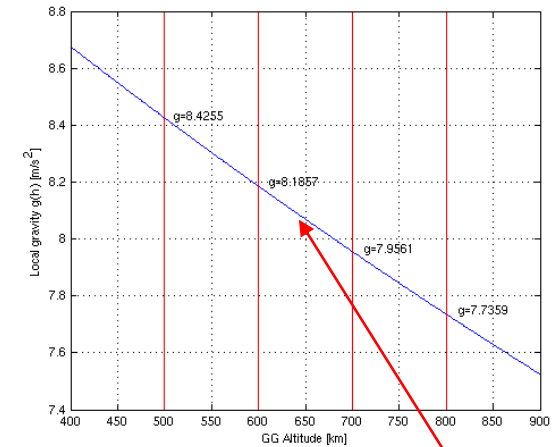
- $A_{s/c} = 2.9 \text{ m}^2$



$h = 630 \text{ km}$ (\approx GPB!)

$g(h) = 8.116 \text{ m/s}^2$

(1)



The Signal

(2)

- Signal optimization: equatorial orbit
 - Inclination depends on the launch site latitude, Kourou → $i \leq 5^\circ$
 - Eccentricity is not zero: $e \leq 0.01$



- Period of longitude variation of ascending node $T_{\text{asc_node}} \approx 48$ days
- Spin axis initially aligned with the orbit angular velocity within $\delta I_0 \leq 1^\circ$
- The angle between the spin axis and the orbit angular velocity changes also due to the gravity gradient and magnetic torque acting on the satellite:

$$\delta I = \delta I_0(\text{launch}) + \delta I_{\text{orbit}} + \delta I_{\text{Torques}} \approx 15\text{-}20^\circ \text{ after about 1-2 years}$$

- But: angle is changing very slowly, each fundamental experiment is carried out with constant driving signal

The Signal

(3)

- Performance check vs. simulated results
- Signal to Noise Ratio
 - The science measurement is: $\Delta x_{EP} = a_{EP} \times (T_{diff})^2 / (4 \times \pi^2)$
 - T_{diff} according to the simulator, $T_{diff} = 500 \text{ s}$
 - Science measurements are affected by systematic errors $d_x(t)$ and by stochastic errors $\tilde{n}(t)$

$$\Delta x'_{EP}(t) = \Delta x_{EP}(t) + d_x(t) + \tilde{n}_x(t)$$

measurement

EP violation signal, $\Delta x_{EP} \approx 0.5 \times 10^{-12} \text{ m}$

- Same allocation (50%) for deterministic and stochastic errors
- Error allocation such that $SNR \geq 2$
- The deterministic effects with the EP signature must be reduced as much as possible: spin modulation “takes away” a lot of disturbances due to the spacecraft (DC effects in the Body Fixed reference frame)
- The stochastic effects define T_{int} : thermal noise (worst case) $\longrightarrow T_{int} \approx 1 \text{ week}$
- Mission duration $\approx 2 \text{ years} \longrightarrow$ Number of $T_{int} \approx 100$ (rich statistics!)

Non Gravitational Forces Acting on the Spacecraft (1)

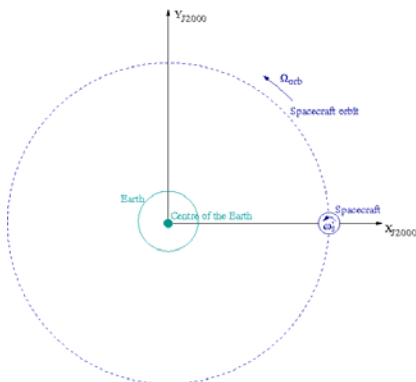
- Non-gravitational forces are sensed as inertial acceleration from test masses \longrightarrow ideally pure common mode, but:
 - test masses mechanical suspension is not ideal \longrightarrow a fraction χ_{CMRRxy} of common mode acceleration is sensed as differential one



- Orbit altitude $h = 630$ km in order to have $a_{NGxy}^{ext} \approx 2 \times 10^{-7} \text{ m/s}^2$
- The Drag Free Control partially compensates the non-gravitational forces (@ orbit frequency in IRF) $\longrightarrow a_{CMxy} = \chi_{DFCxy} \times a_{NGxy}^{ext}$



- ✓ reduced mechanical balance requirement for the capacitance bridge
- ✓ reduced inertial acceleration acting on PGB, i.e. smaller displacement
- ✓ reduced test masses common mode acceleration, i.e. smaller displacement



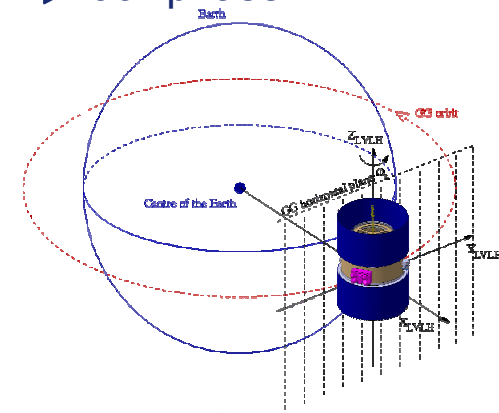
Non Gravitational Forces Acting on the Spacecraft

- Main non-gravitational force component along Y_{LVLH} \longrightarrow 90° phase difference wrt EP signal, SNR = 2

$$a_{NGxy}^{ext} \times \chi_{DFCxy} \times \chi_{CMRRxy} \leq a_{EP} \times 1/SNR$$

$$\chi_{CMRRxy} \leq 10^{-5}$$

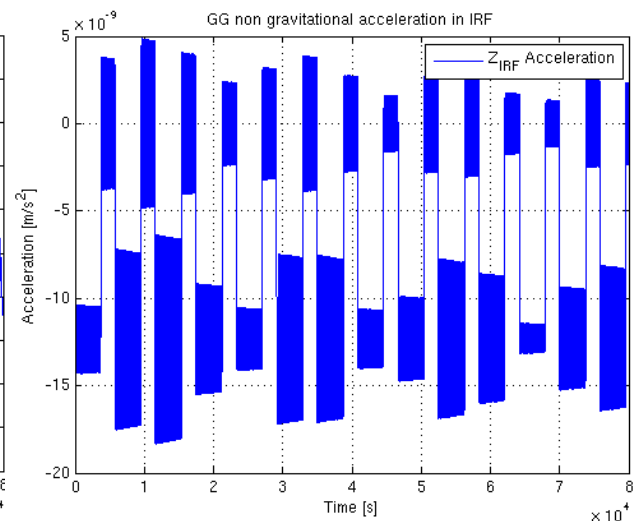
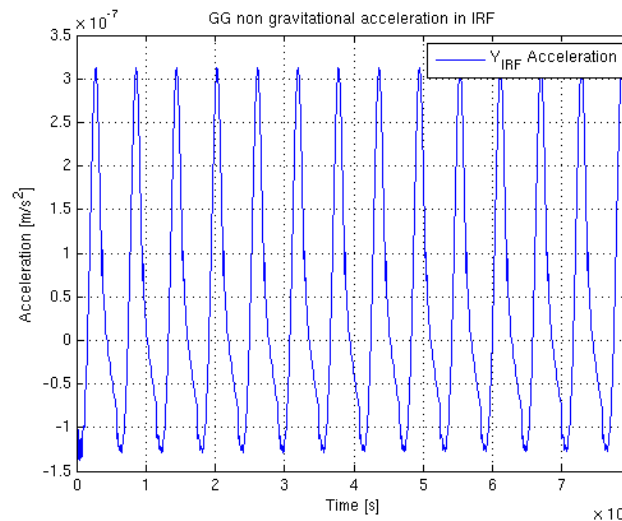
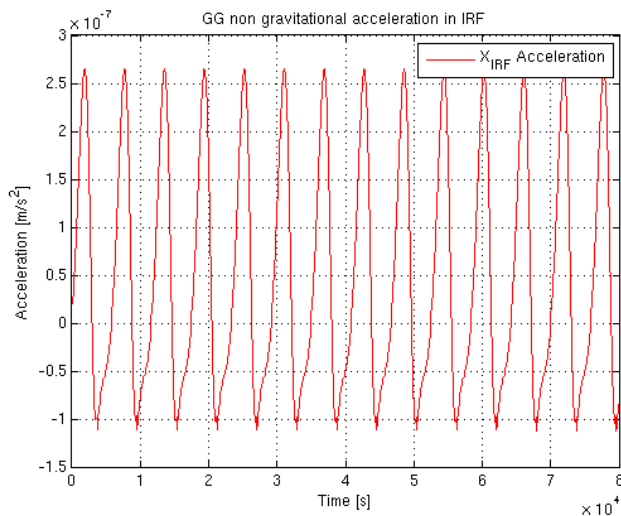
$$\chi_{DFCxy} \leq 2 \times 10^{-5}$$



- Maximum inertial acceleration sensed from PGB $a_{CMxy} = 4 \times 10^{-12} \text{ m/s}^2$
- PGB XY_{plane} oscillation period $T_{PGBxy} \sim 381.24 \text{ s}$ \longrightarrow displacement \ll capacitance gap, whirl period is slow
- TM XY_{plane} common mode period $T_{CM} = 104.17 \text{ s}$ \longrightarrow TM displacement \ll capacitance gap, whirl period is slow
- Mechanical balance of capacitance bridge $\chi_{bridge} (T_{CM} = 104 \text{ s}) = 6 \times 10^{-4}$ \longrightarrow $a-b \ll 3 \text{ } \mu\text{m}$ over a gap $a \approx 5 \text{ mm}$

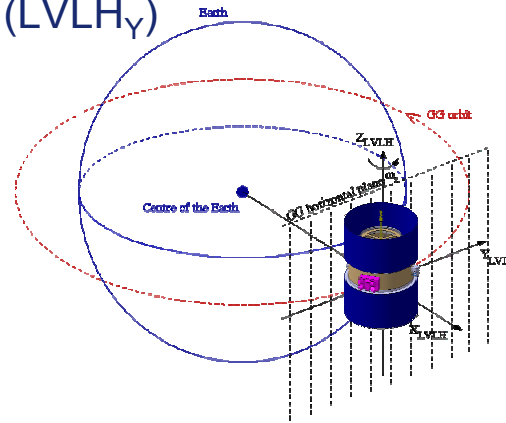
Non Gravitational Forces Acting on the Spacecraft (in IRF) (3)

- Non-gravitational acceleration time series (frozen values for $m_{s/c}$ and $A_{s/c}$)
 - Date: 2013 July 12th
 - GG altitude $h = 630$ km
 - Atmospheric model: MSIS '86 (above 120 km MSIS '86 = MSIS2000)
 - Solar radiation included (F10=180, F10B=160, Geomagnetic Index = 8)



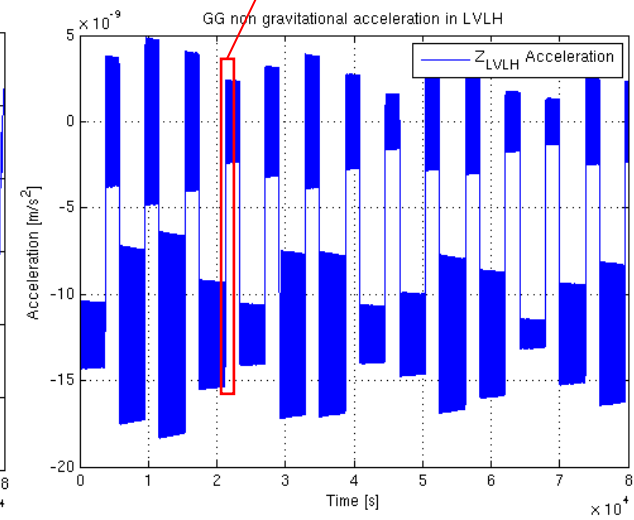
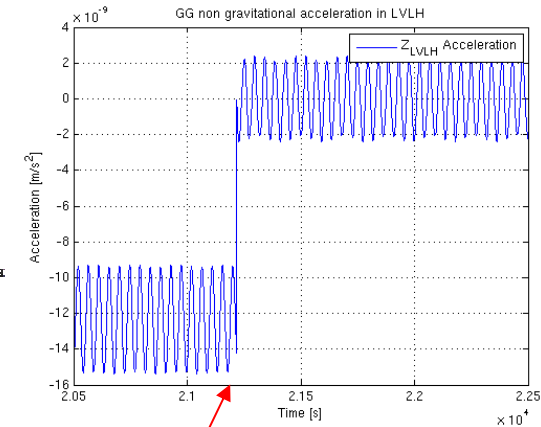
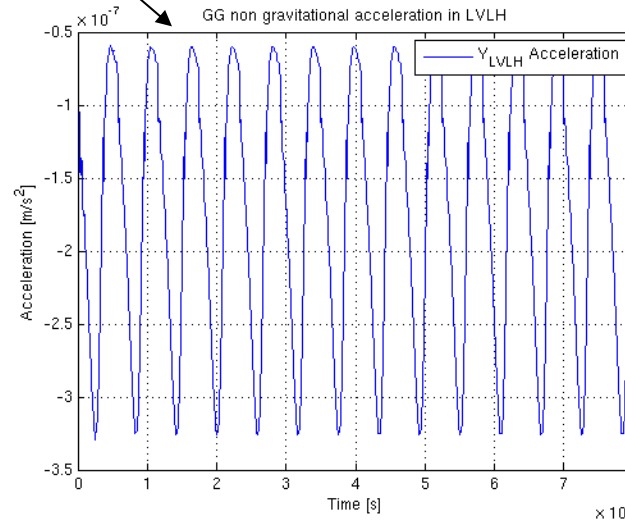
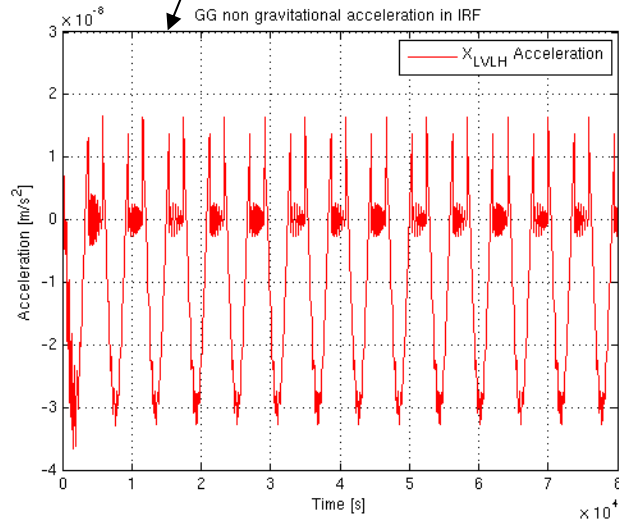
Non Gravitational Forces Acting on the Spacecraft (in LVLH) (4)

- Main component along track ($LVLH_Y$)



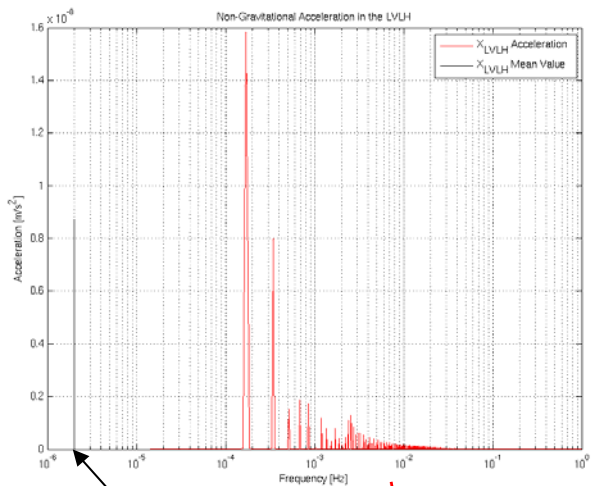
Radial NG_X
acceleration

Along track NG_Y
acceleration



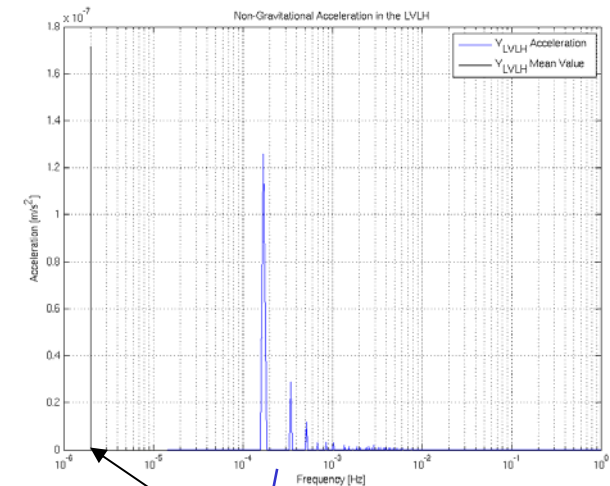
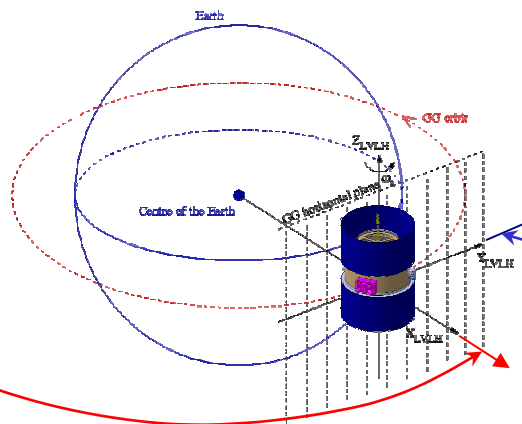
Non Gravitational Forces Acting on the Spacecraft (5)

- Main non-gravitational acceleration component along Y_{LVLH} $\longrightarrow 90^\circ$ phase difference wrt EP signal, but SNR = 2 ...



mean value of a_{LVLHx}
Like EP violation!!

The EP violation signal is **always along X in the LVLH Frame** and almost constant during an elementary science experiment.

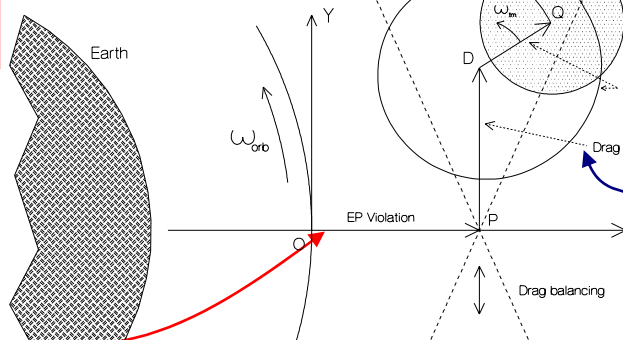
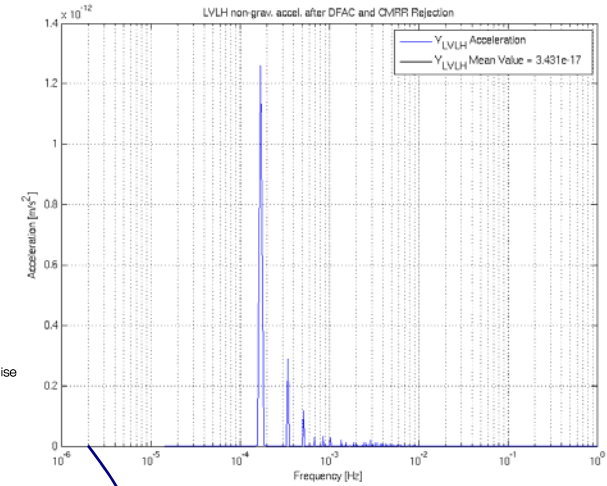
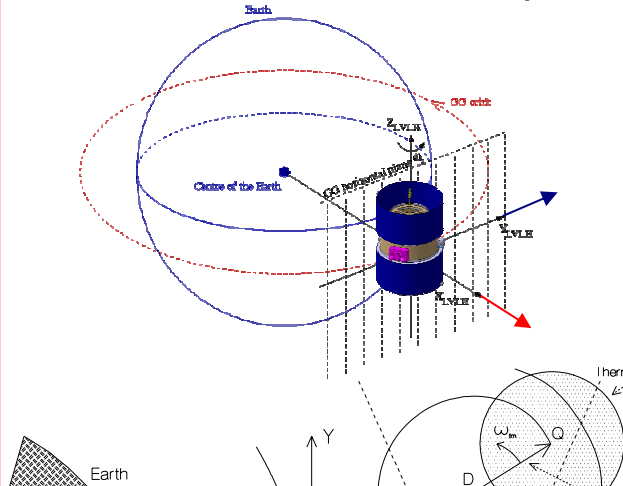
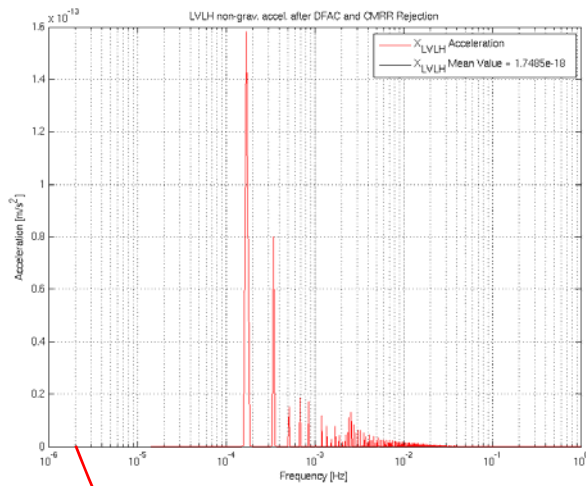


mean value of a_{LVLHy}
Like EP violation, but 90° out of phase!!

Non Gravitational Forces Acting on the Spacecraft

(6)

- Main non-gravitational acceleration after DFC compensation and suspension rejection – CMRR- fulfills the requirement



$dx_{ang} = 0.011 \text{ pm}$

$dy_{ang} = 0.217 \text{ pm}$

The Gravitational Forces

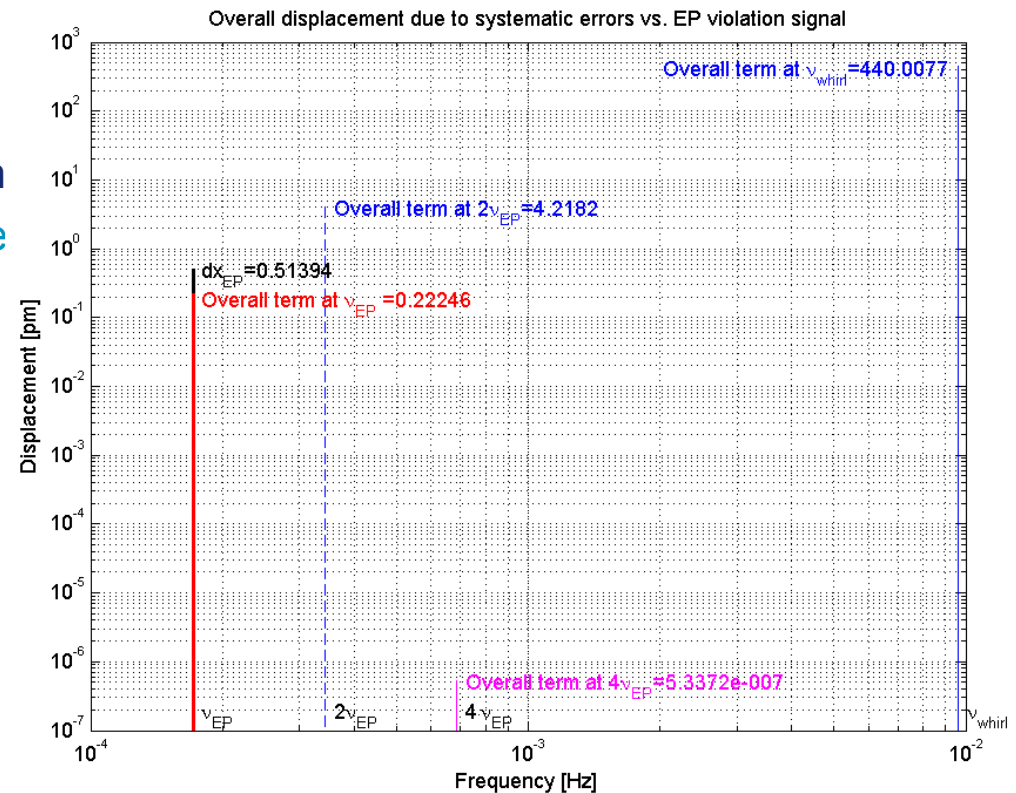
- TM higher mass moment coupling with Earth monopole
 - TM quadrupole mass moment couples with Earth monopole
- ↓
- Inner TM $\delta J_i/J_i = -0.0116$ Outer TM $\delta J_o/J_o = -0.0065$
 - Test masses quadrupole are both small and of the same order
- Differential acceleration = $9.3 \times 10^{-18} \text{ m/s}^2 \approx 0.1 \times a_{EP}$

- Tidal effects (displacements on XY plane)
 - Gravity gradient T_{jj} magnitude corresponding to the GG local gravity:
 $T_{jj}(h_{GG}) = 3 \times 10^{-6} \text{ m/s}^2/\text{m}$ $T_{jk}(h_{GG}) = 3 \times 10^{-7} \text{ m/s}^2/\text{m}$ (worst case)
 - Signature difference with respect to EP signal
- ↓

During science measurement the TM whirl radius r_w must not affect the EP signal detection (through T_{jj}): $\longrightarrow r_w \leq 5 \times 10^{-10} \text{ m}$

GG Error Budget (according to simulator parameters) (1)

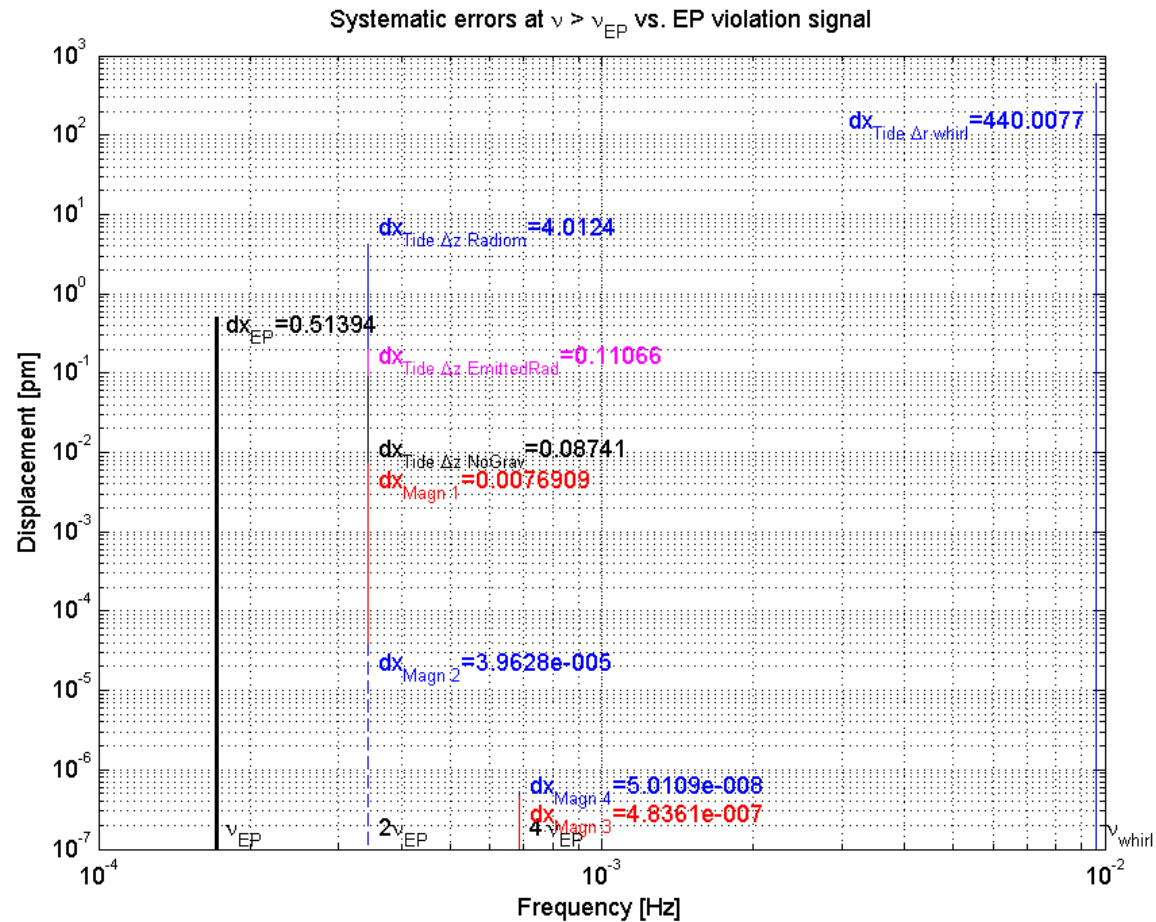
- Amplitude Spectrum of EP signal and disturbing effects (affecting measurements in the XY plane) as observed in the IRF
- Signal and most effective deterministic disturbances (smallest frequency separation)
 - Most effecting disturbance at ν_{EP} , well below the signal
 - One week duration of the elementary experiment ensures good frequency separation for all the competing lines, also the first one at $2 \times \nu_{EP}$



GG Error Budget

(2)

- Detailed error budget for the first lines of deterministic forces affecting GG.



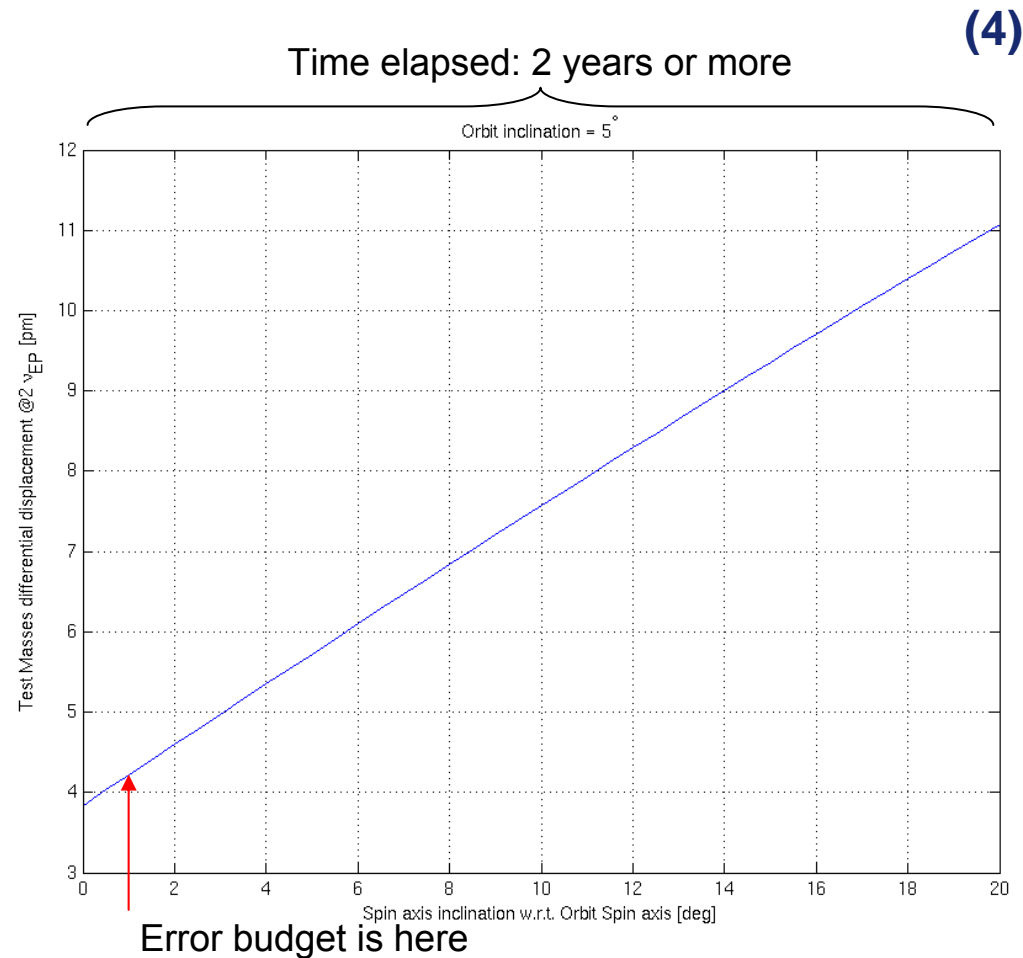
GG Error Budget

(3)

Acceleration (transverse plane) due to:	Frequency in IRF (Hz)	Frequency in BF (Hz)	Phase	Differential acceleration (m/s ²)	Differential displacement (pm)
EP signal	v_{orb}	v_S (wrt Earth)	X_{LVLH}	$8.116 \cdot 10^{-17}$	0.51
External non gravitational forces	v_{orb}	v_S	Mainly along Y_{LVLH}	$1.7 \cdot 10^{-7}$	-
External non gravitational forces after DFC compensation and CMRR	v_{orb}	v_S	Mainly along Y_{LVLH}	$3.4 \cdot 10^{-17}$	0.22
Earth coupling with TMs quadrupole moments	v_{orb}	v_S	X_{LVLH}	$9 \cdot 10^{-18}$	0.06
Radiometric effect along Z coupled with Earth tide	$2 \cdot v_{orb}$	$v_S \pm v_{orb}$	X_{LVLH}	$6.3 \cdot 10^{-16}$	4.0
Emitted radiation along Z coupled to Earth tide	$2 \cdot v_{orb}$	$v_S \pm v_{orb}$	X_{LVLH}	$4 \cdot 10^{-17}$	0.11
Tide coupled to non grav. acceleration along Z	$2 \cdot v_{orb}$	$v_S \pm v_{orb}$	X_{LVLH}	$1.4 \cdot 10^{-17}$	0.09
TM1 inner magnetic dipole coupled to B_{\oplus} magnetized TM2	$2 \cdot v_{orb}$	$v_S \pm v_{orb}$	X_{LVLH}	$1 \cdot 10^{-18}$	$8 \cdot 10^{-3}$
TMs inner magnetic dipoles coupled to B_{\oplus}	$2 \cdot v_{orb}$	$v_S \pm v_{orb}$	X_{LVLH}	$6 \cdot 10^{-21}$	$4 \cdot 10^{-5}$
TM1 and TM2 with B_{\oplus} induced magnetization couple	$4 \cdot v_{orb}$	$v_S \pm 3 \cdot v_{orb}$	X_{LVLH}	$8 \cdot 10^{-23}$	$5 \cdot 10^{-7}$
TM1 with B_{\oplus} induced magnetization couples with B_{\oplus}	$4 \cdot v_{orb}$	$v_S \pm 3 \cdot v_{orb}$	X_{LVLH}	$8 \cdot 10^{-24}$	$5 \cdot 10^{-8}$
Whirl motion coupled to Earth tide	$v_w, v_w \pm 2 \cdot v_{orb}$	$\approx v_S \pm v_w$ ($v_{orb} \ll v_w$)	X_{LVLH}	$6.9 \cdot 10^{-14}$	440
...	Higher frequencies	Frequencies far from v_S	X_{LVLH}

GG Error Budget

- Variation of line @ $2v_{EP}$ due to the change of the angle in between spin axis and orbit angular rate
 - Variation very slow in time (signal and line are almost constant during one week)
 - 11 pm can be distinguished very well with one week of continuous data



GG Error Budget

(5)

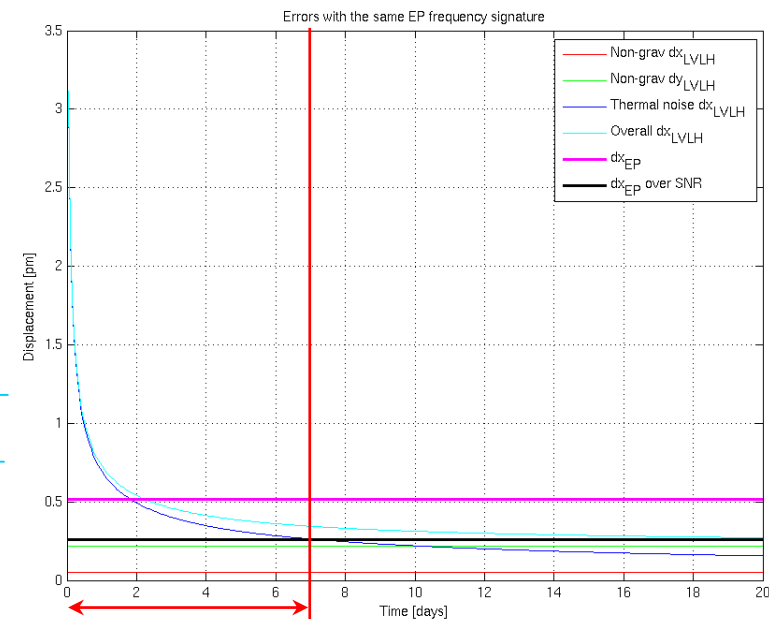
- Thermal noise due to TMs “spring” dissipation ($Q_{TM} = 20000$) directly affects the science measurement (it is the main stochastic disturbance):

$$SD(\tilde{n}_{TM-th}) = \sqrt{\frac{4K_B T \cdot \omega_{DM}}{m_{TM} \cdot Q_{TM}}} \quad \longrightarrow \quad T_{int} \approx 1 \text{ week}$$

- Overall dx_{LVLH} takes into account deterministic and stochastic contribution

$$SD(\tilde{n}_{TM-th}) = 3.2 \cdot 10^{-14} \text{ m/s}^2/\sqrt{\text{Hz}}$$

$$\text{Overall } dx_{LVLH} = \sqrt{(dx_{LVLH})^2 + (dy_{LVLH})^2 + \frac{SD^2(\tilde{n}_{TM-th})}{T_{int} \cdot \omega_{DM}^4}}$$



T_{int} : elementary
experiment duration

Simulator for GG spinning @1 Hz

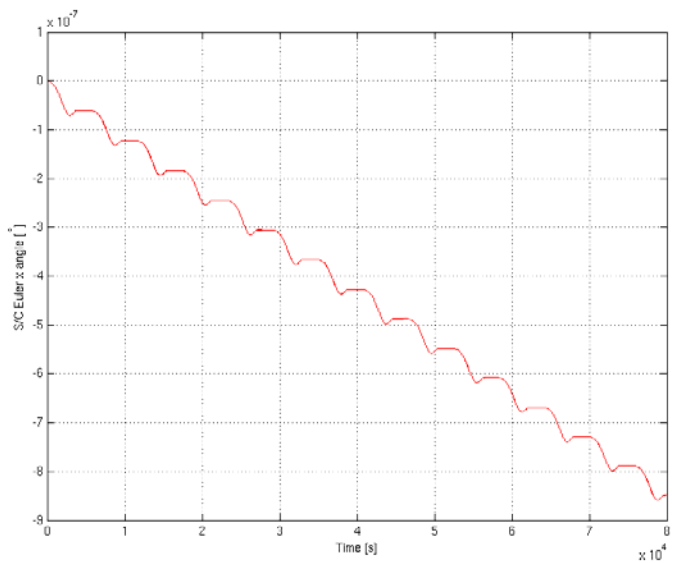
(1)

- Spacecraft shell, PGB, TMi, TMo, dummy body for not solving the orbit motion in a rapidly spinning reference frame: **27 DoFs**
- Gravity and gravity gradient are “on”
- Current mass/inertia properties for all bodies (included proof masses quadrupole moment)
- Orbit altitude $h = 630$ km to match the reference non gravitational acceleration **$2 \times 10^{-7} \text{ m/s}^2$**
- Stiffness are reproducing PGB modes and common and differential proof masses modes in the XY plane and along Z according to the mission requirements
- Mechanical quality factor is lowered for TMs in order to amplify whirl motion
- Environment fully modeled
- **$\eta = 10^{-17}$** for all the science simulations (science target)
- **Quadruple precision** simulations are carried out in order to predict science performance of the mission

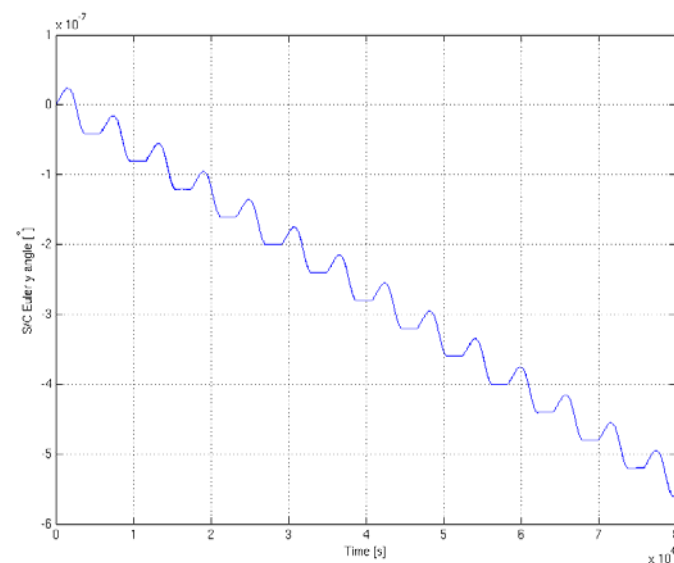
Simulator for GG spinning @1 Hz

(2)

- DFC, AOCS and PGB-s/c control in open loop
- PGB and TMs whirl control in closed loop



s/c to LVLH hinge attitude angle x
time series



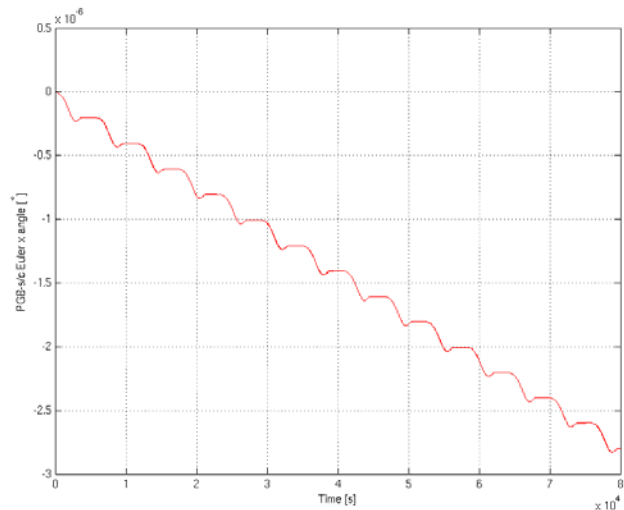
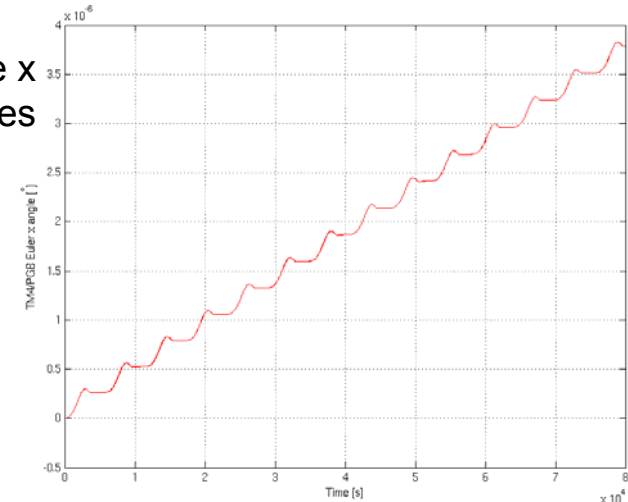
s/c to LVLH hinge attitude angle y
time series

s/c to LVLH hinge attitude angle z
time series is ωt

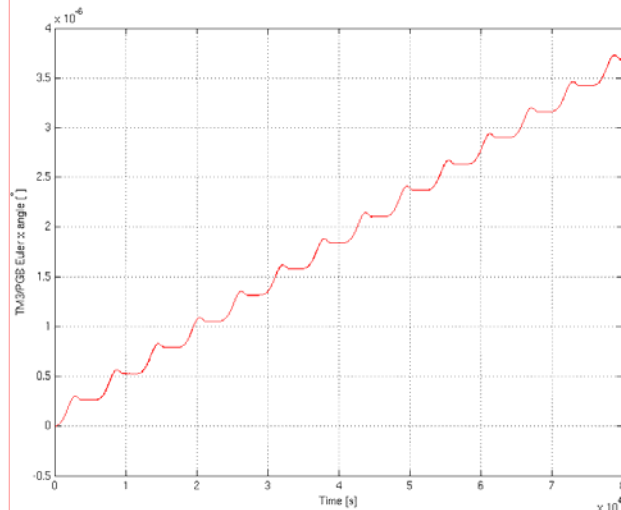
Simulator for GG spinning @1 Hz

(3)

TM4-PGB hinge attitude angle x time series

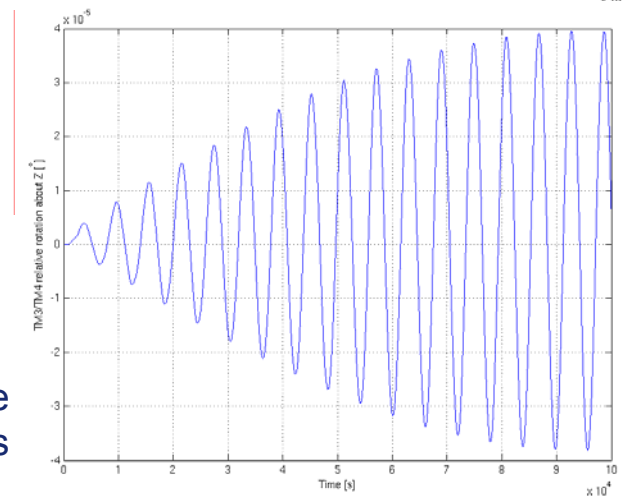


PGB-s/c hinge attitude angle x time series



TM3-PGB hinge attitude angle x time series

TM3-TM4 differential angle z time series



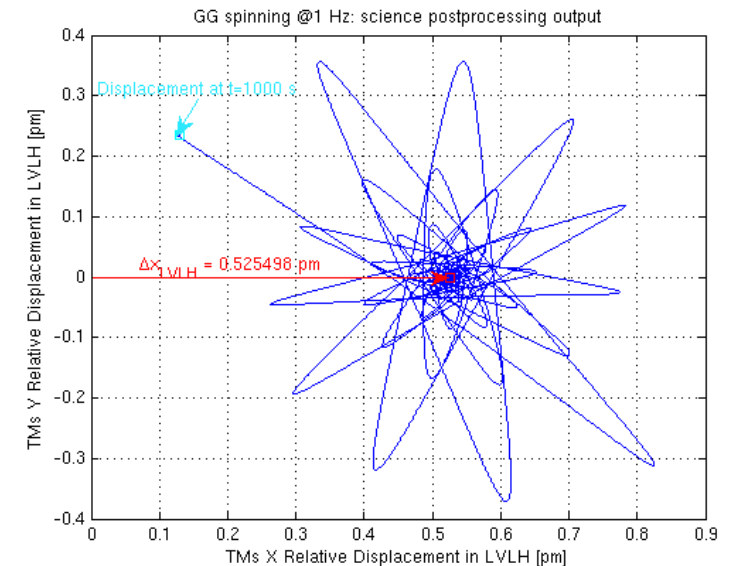
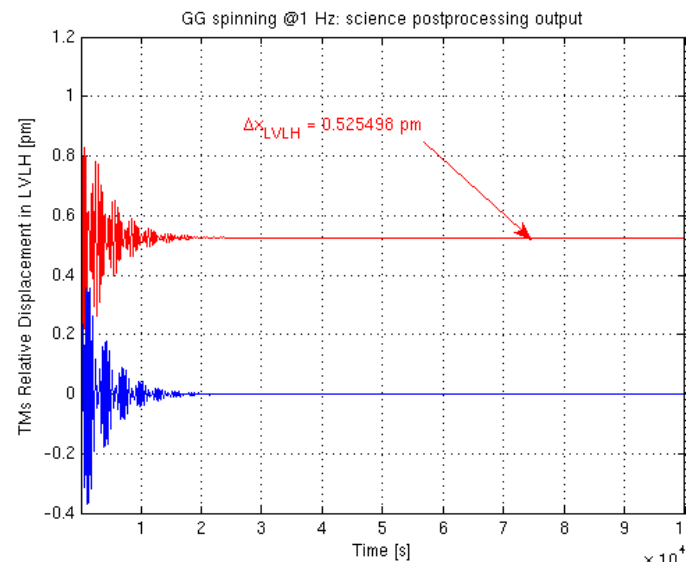
Simulator for GG spinning @1 Hz (4)

- 1 Hz is better for the simulator... CPU time is reduced by a factor 2
- Changing spin frequency modifies dynamics, changing η modifies F_{EP} strength... but

Predicted value:
$$\Delta x_{LVLH} = \frac{F_{EP}}{m_{TM} \cdot \left(\omega_{DM}^2 - 3 \cdot \frac{GM_{\oplus}}{(R_{\oplus} + h)^3} \right)} = 5.25501 \cdot 10^{-13} \text{ m}$$

“Measured” value: $\Delta x_{LVLH} = 5.25498 \cdot 10^{-13} \text{ m !!}$

Time series of the TMs differential displacement in the LVLH Reference Frame



Polar plot of the TMs differential displacement in the LVLH Reference Frame

After a transient the TMs relative position has almost null mean value along Y_{LVLH} and 0.525 pm mean value along X_{LVLH}