

# An accelerometer for spaceborne applications with interferometric readout: **test of LIG performances**

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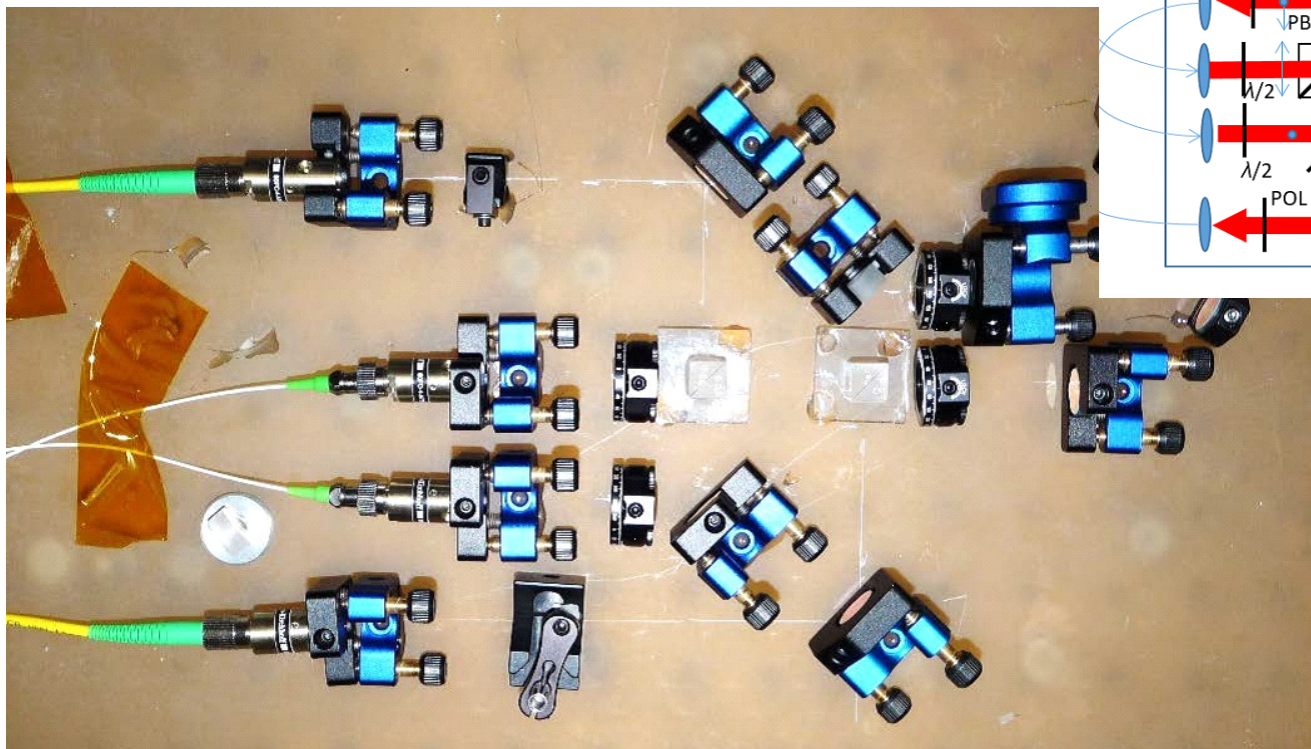




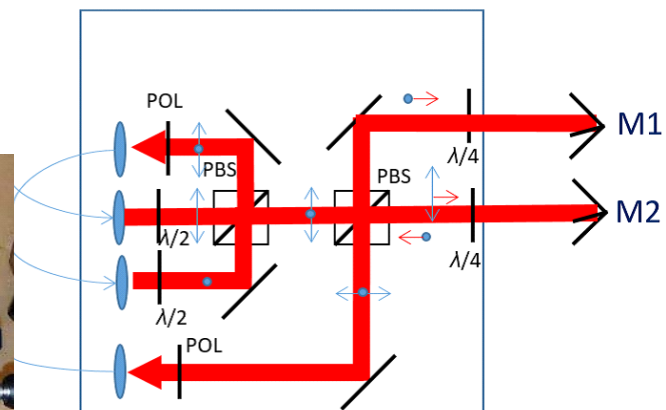
# Test of the performances

- Resolution/noise test
- Accuracy/non-linearity test

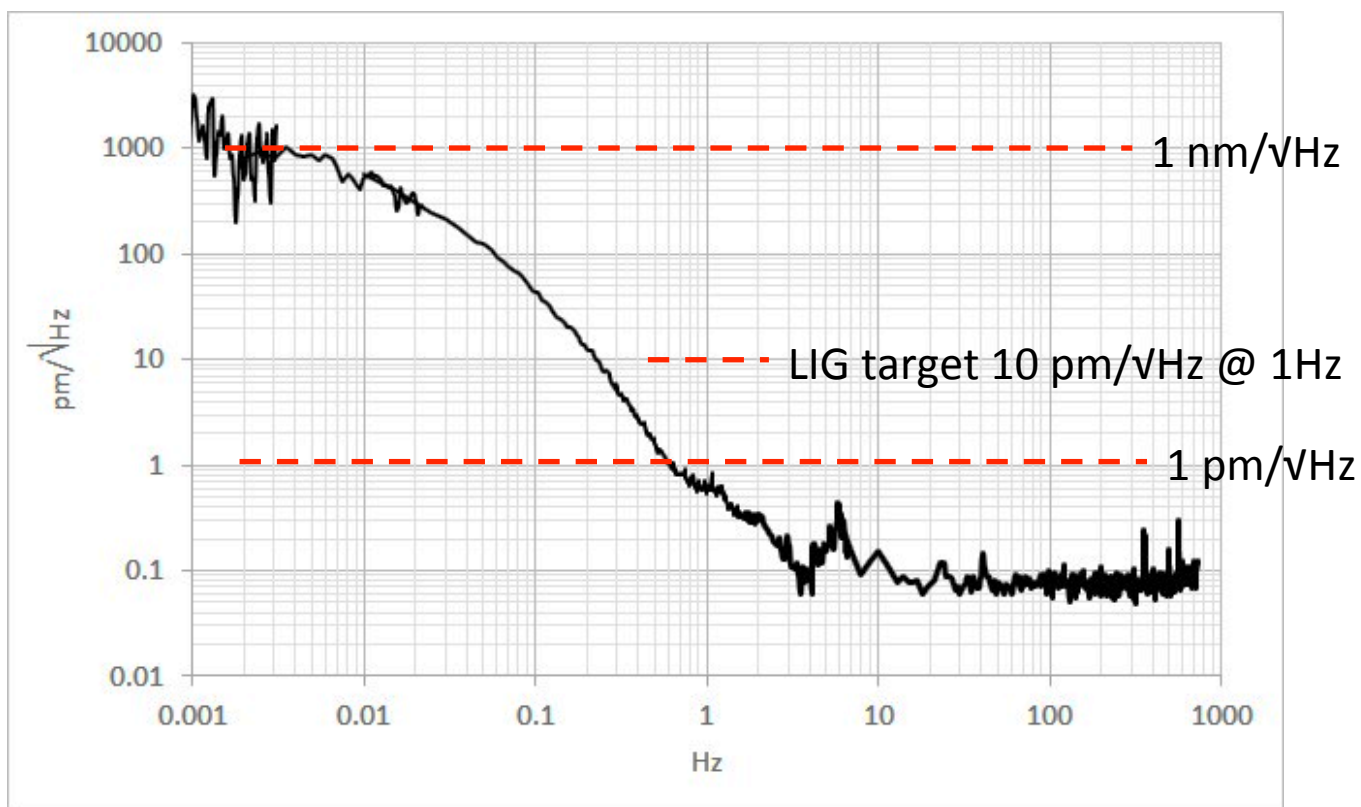
# Resolution/noise test



Optical head



# LIG displacement noise

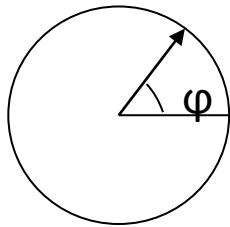




# How to measure the accuracy?

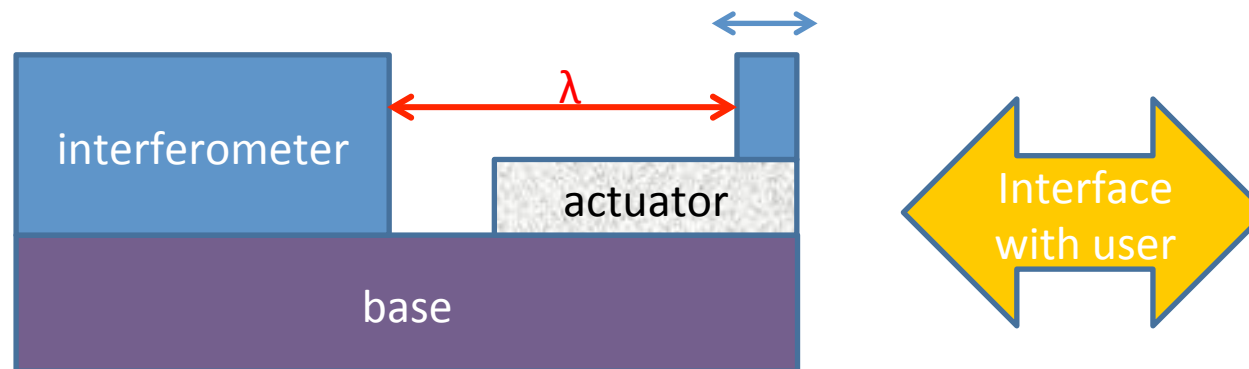
We need a **super-linear super high resolution** reference actuator!

We made it and called Pico Reference Actuator (PRA)

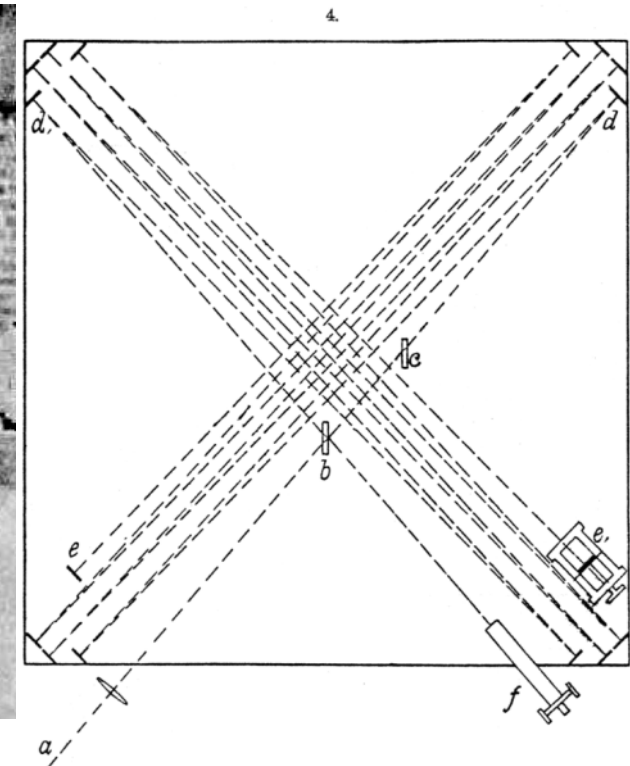
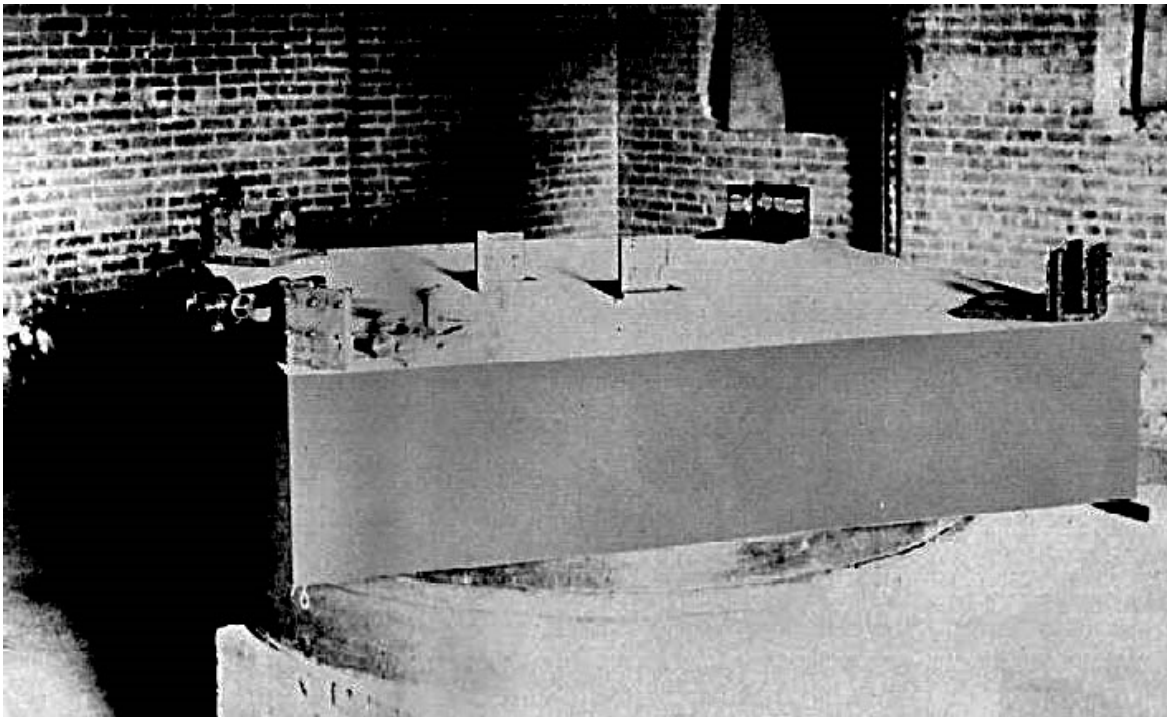


# PRA working principle

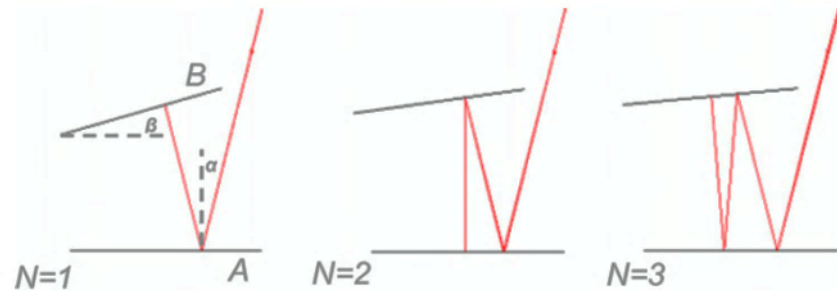
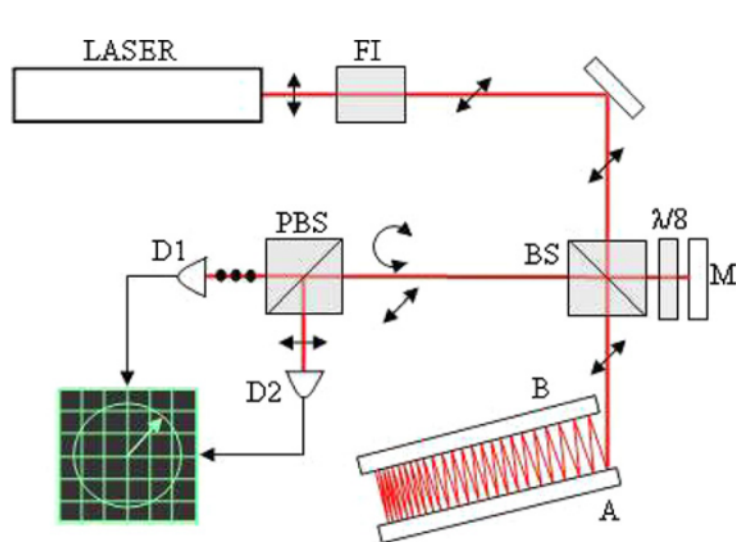
Linear actuator + extremely high resolution interferometer



# Multiple reflection set-up 1888

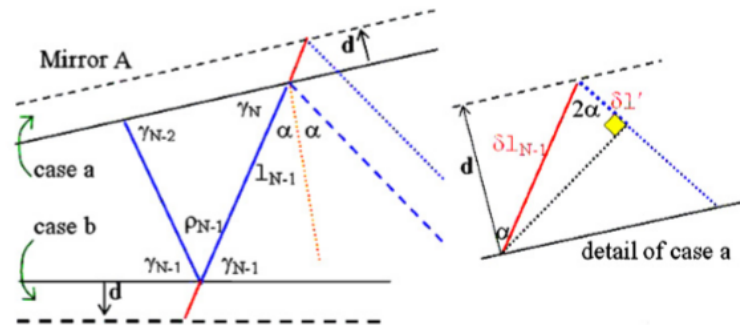
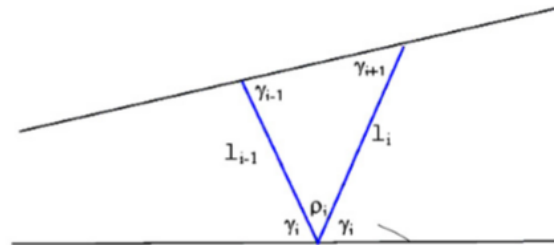


# Multi-reflection interferometer



- The measurement beam of the interferometer is reflected  $N$  times between two mirrors
- The optical path change is the **displacement multiplied by a factor  $N$**
- Almost true...

# Correction parameter



$$\alpha = \rho_N/2 = N\beta. \quad (2)$$

From equation (1) we have that  $l_{N-1}$ , the length of the last path entirely contained between the two mirrors, is related to  $l_0$  as follows:

$$l_{N-1} = l_0 s_1 / (s_{N-1} s_N) \quad \text{or} \quad l_0 = l_{N-1} s_N / s_1. \quad (3)$$

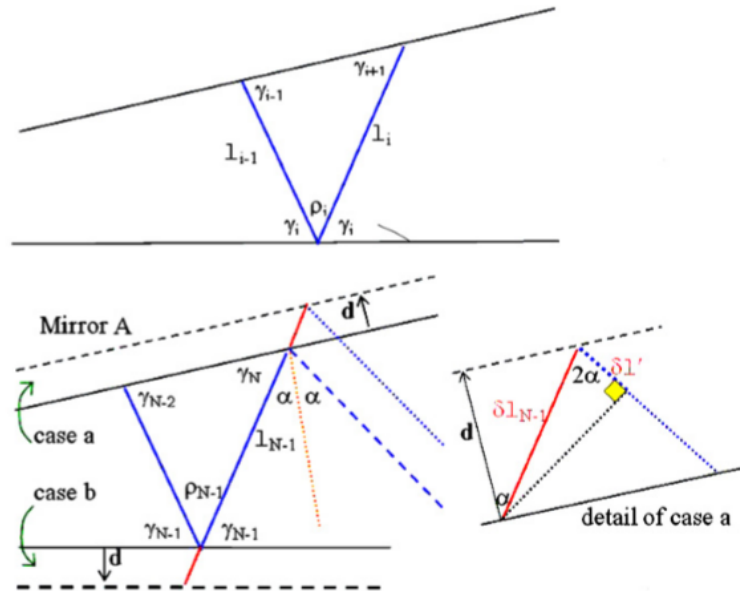
After defining

$$K(N, \alpha) = \sum_{i=0}^{N-1} 1/(s_i s_{i+1}), \quad (4)$$

we then have an exact expression for the total 'internal' pathlength  $L$

$$\begin{aligned} L^{\text{int}} &= 2(l_0 + l_1 + l_2 + \dots + l_{N-1}) \\ &= 2l_0 s_1 K = 2l_{N-1} s_{N-1} s_N K. \end{aligned} \quad (5)$$

# Correction parameter



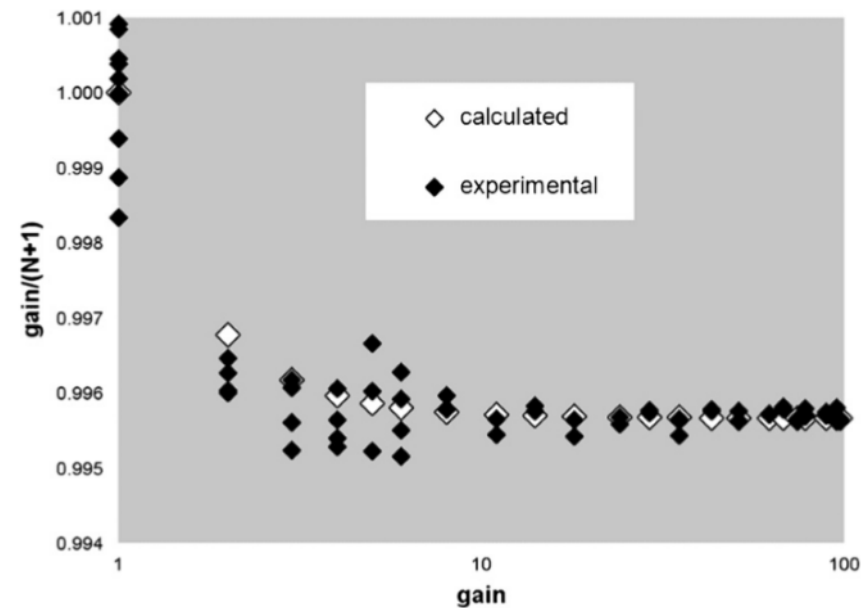
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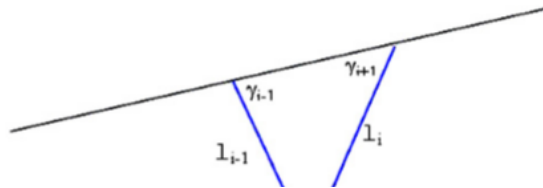
$l_{N-1}$

After def

we then  
pathlength



# Correction parameter



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1.001

IOP PUBLISHING

Meas. Sci. Technol. 20 (2009) 084008 (6pp)

MEASUREMENT SCIENCE AND TECHNOLOGY

[doi:10.1088/0957-0233/20/8/084008](https://doi.org/10.1088/0957-0233/20/8/084008)

## A homodyne Michelson interferometer with sub-picometer resolution

Marco Pisani

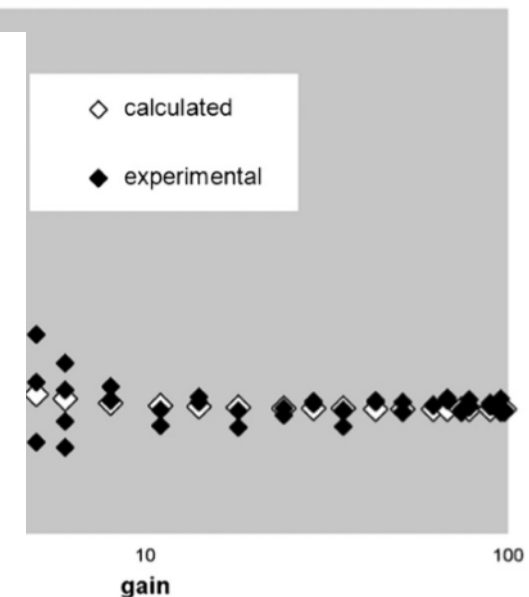
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Received 24 November 2008, in final form 12 January 2009

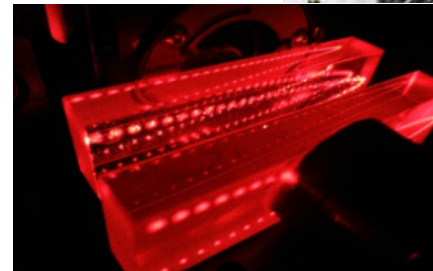
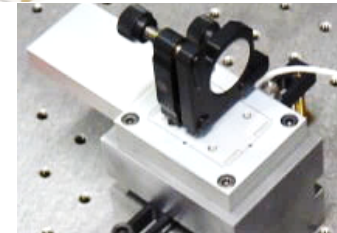
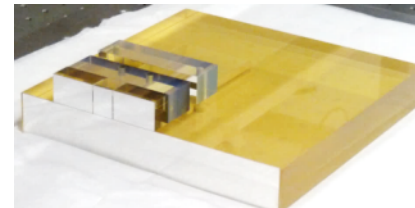
Published 30 June 2009

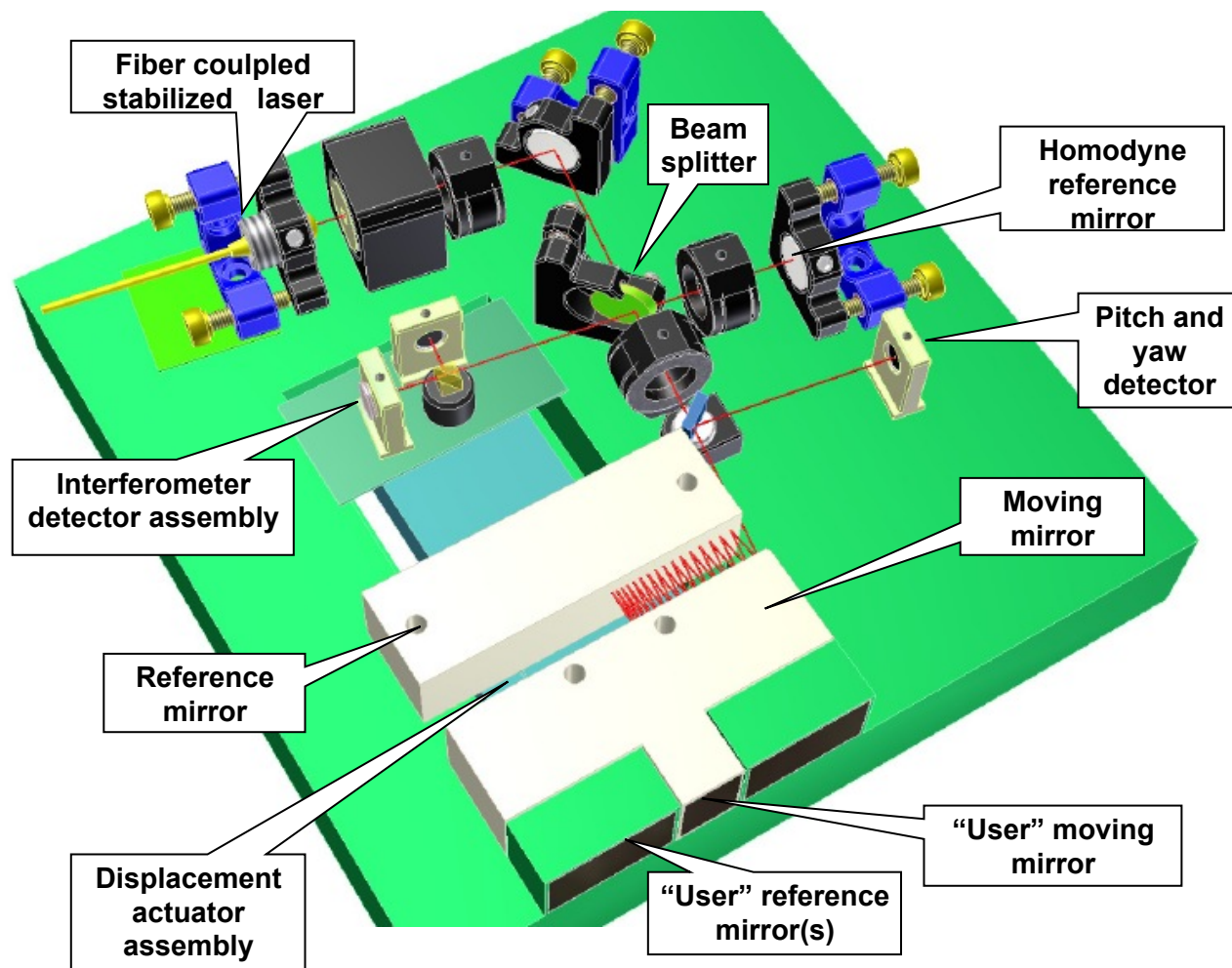
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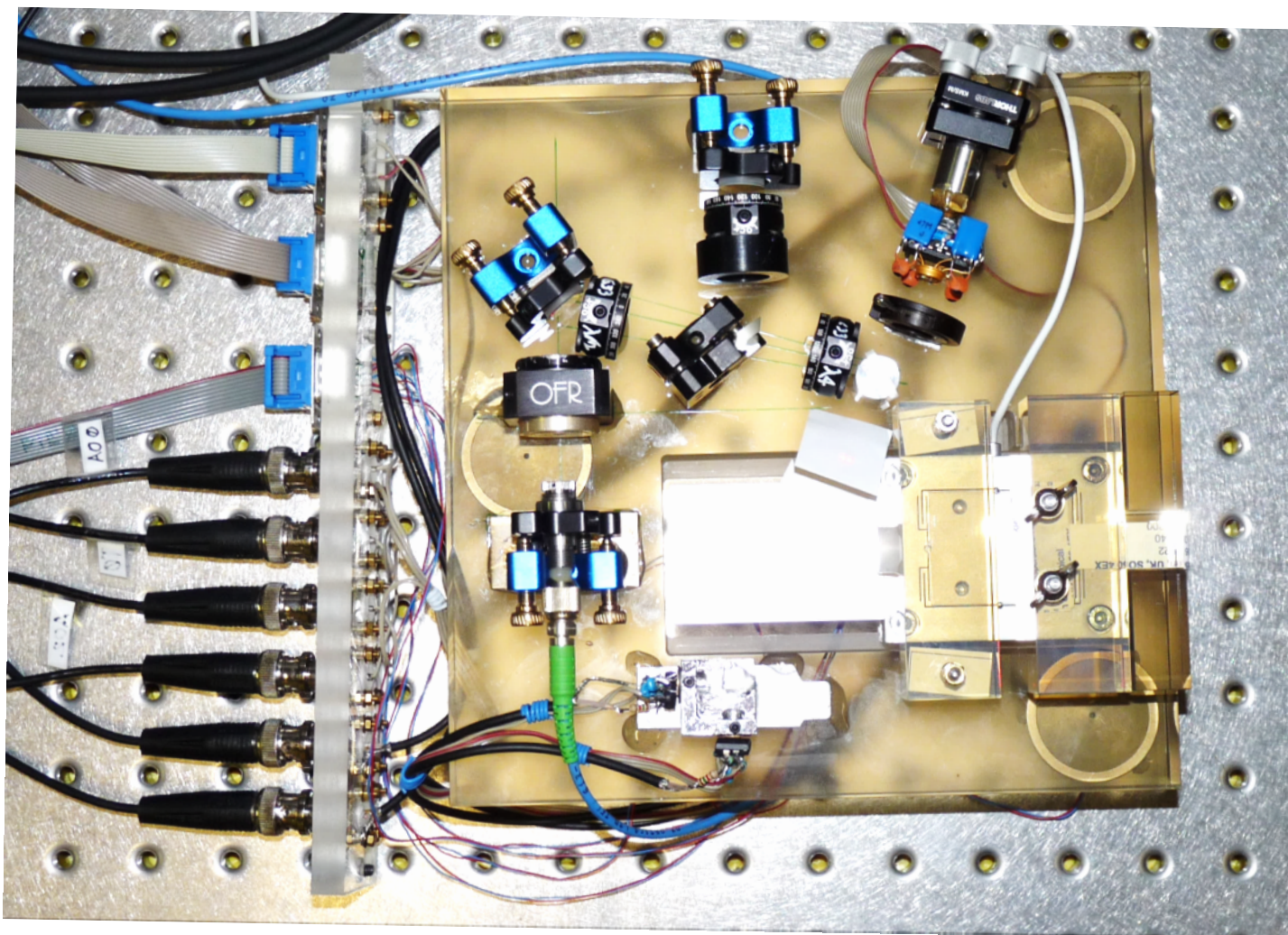


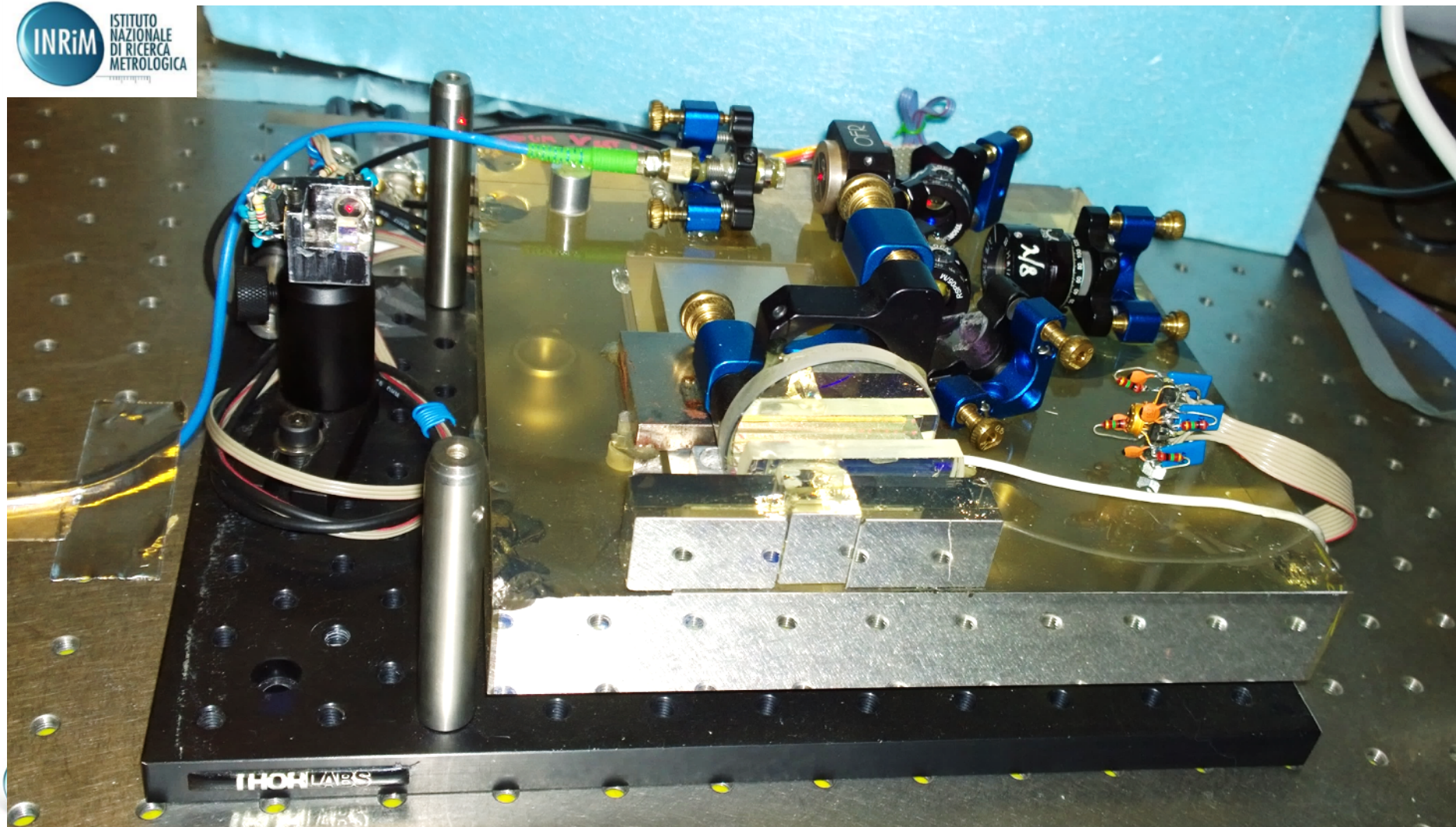
# Practical realization

- The structure is made of Clearceram (low CTE)
- The actuator is a piezo driven flexure stage with 100  $\mu\text{m}$  stroke and integrated metrology (MCL NanoOP100)
- Two high reflectivity ( $R > 99.5\%$ ) mirrors as optical path multiplier



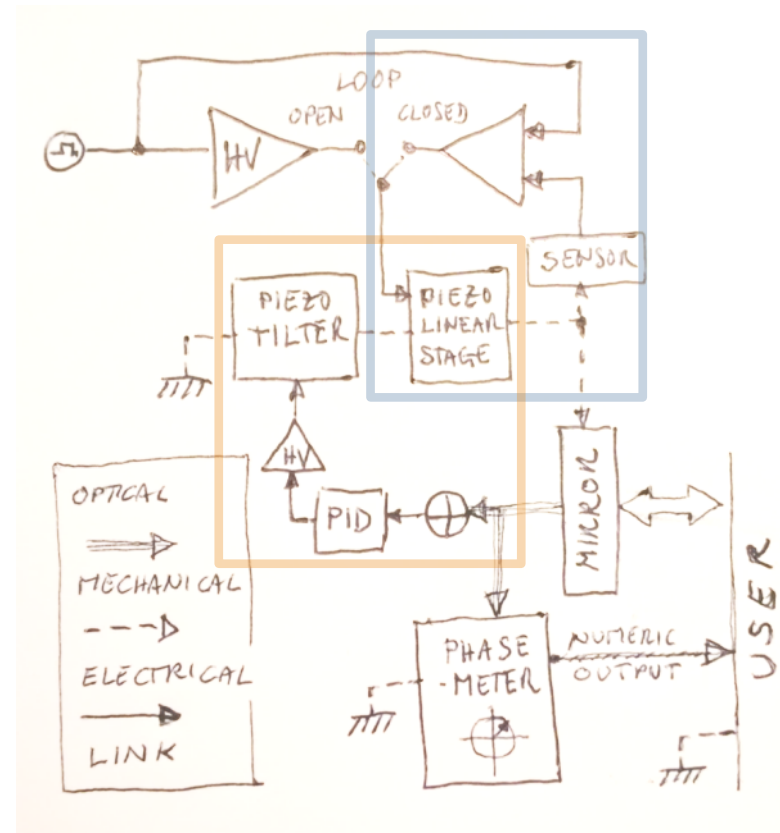






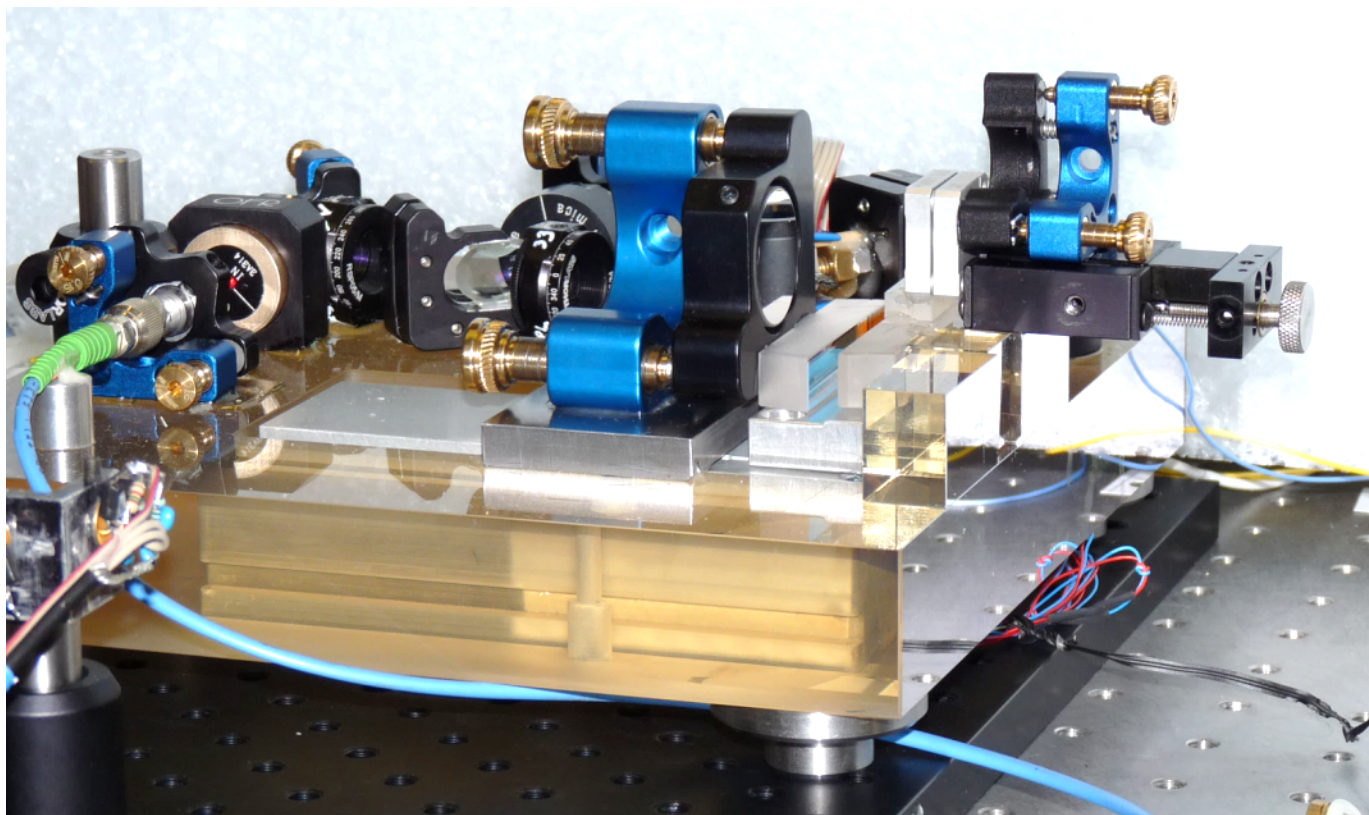
# Opto-electro-mechanic simplified scheme

- Open loop: the piezo actuator is driven with a low noise voltage source with an «unknown» amplitude.
- Closed loop: the piezo actuator makes use of its own metrology system and is driven in a more deterministic way. More noisy.
- In both cases the output of the device is the interferometer reading.

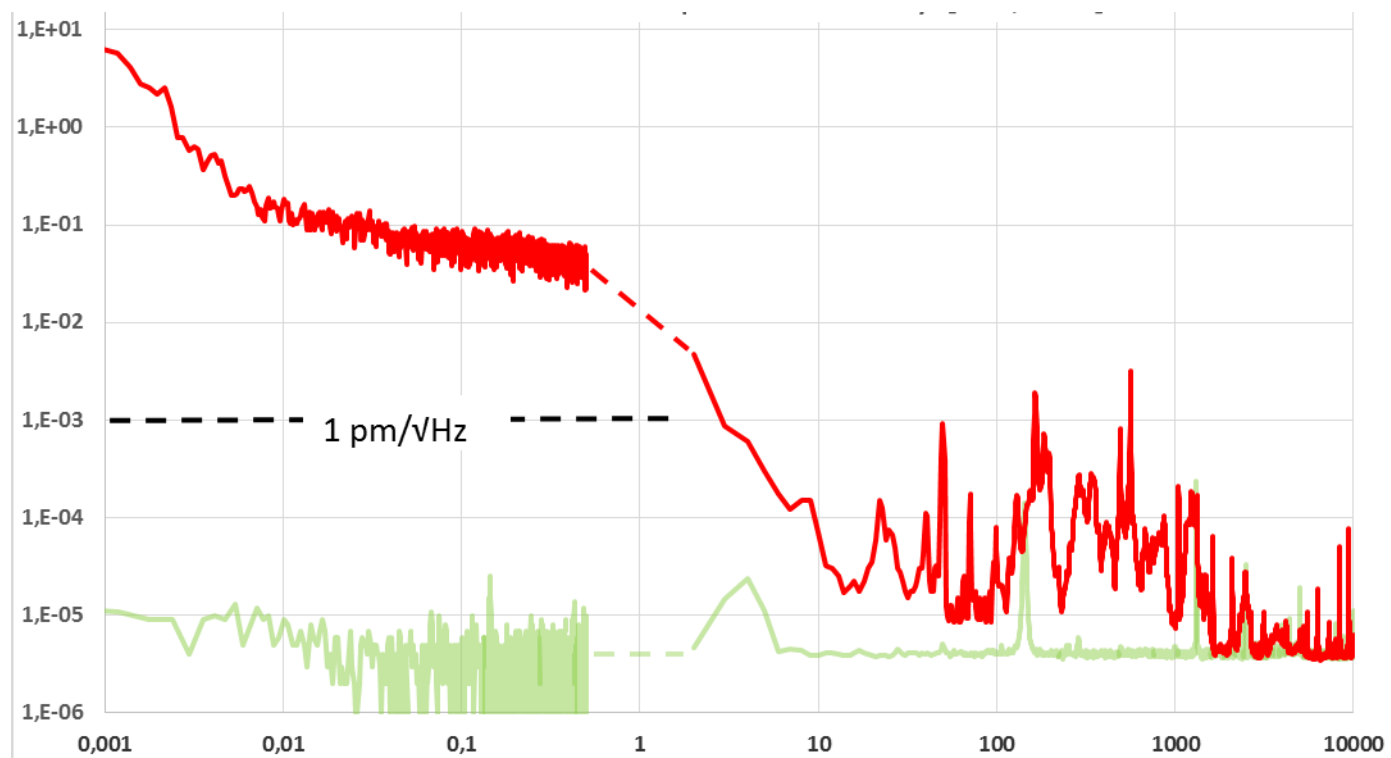


# Example of application

Calibration of a capacitive sensor: one of the electrodes is glued to the moving mirror

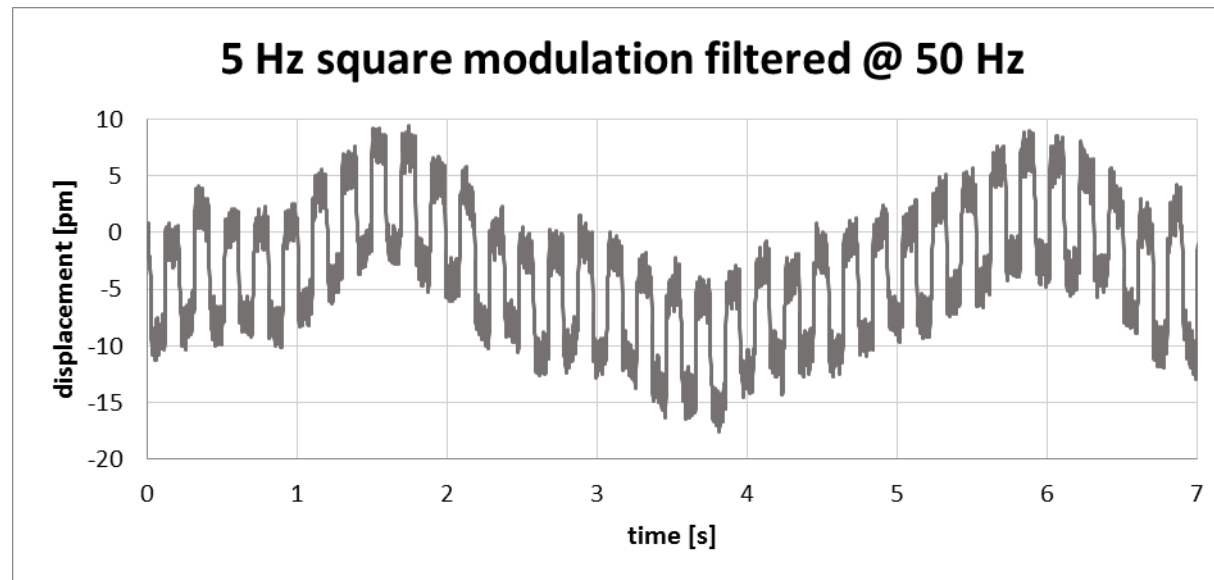


# PRA displacement noise test (nm/√Hz)

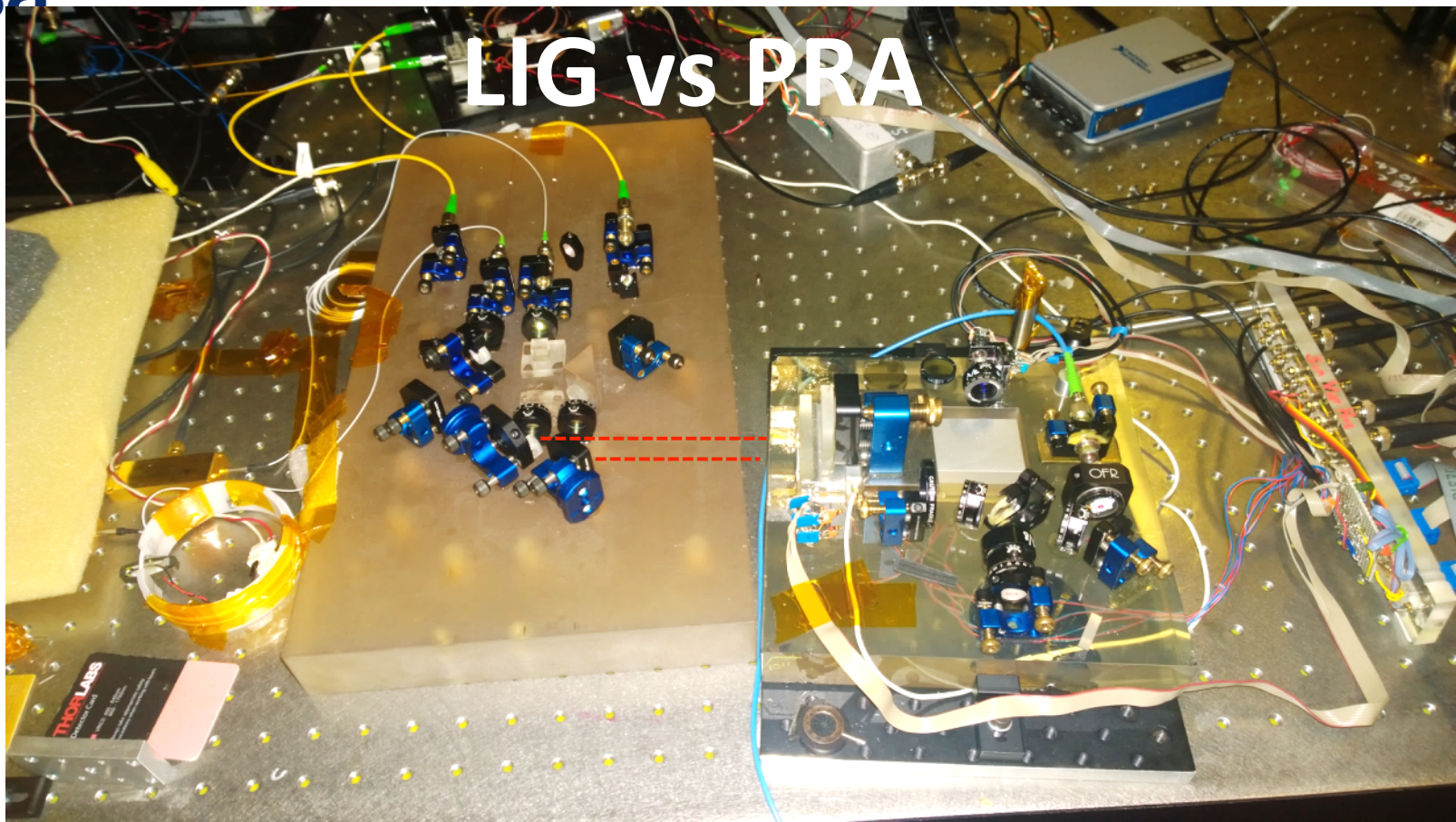


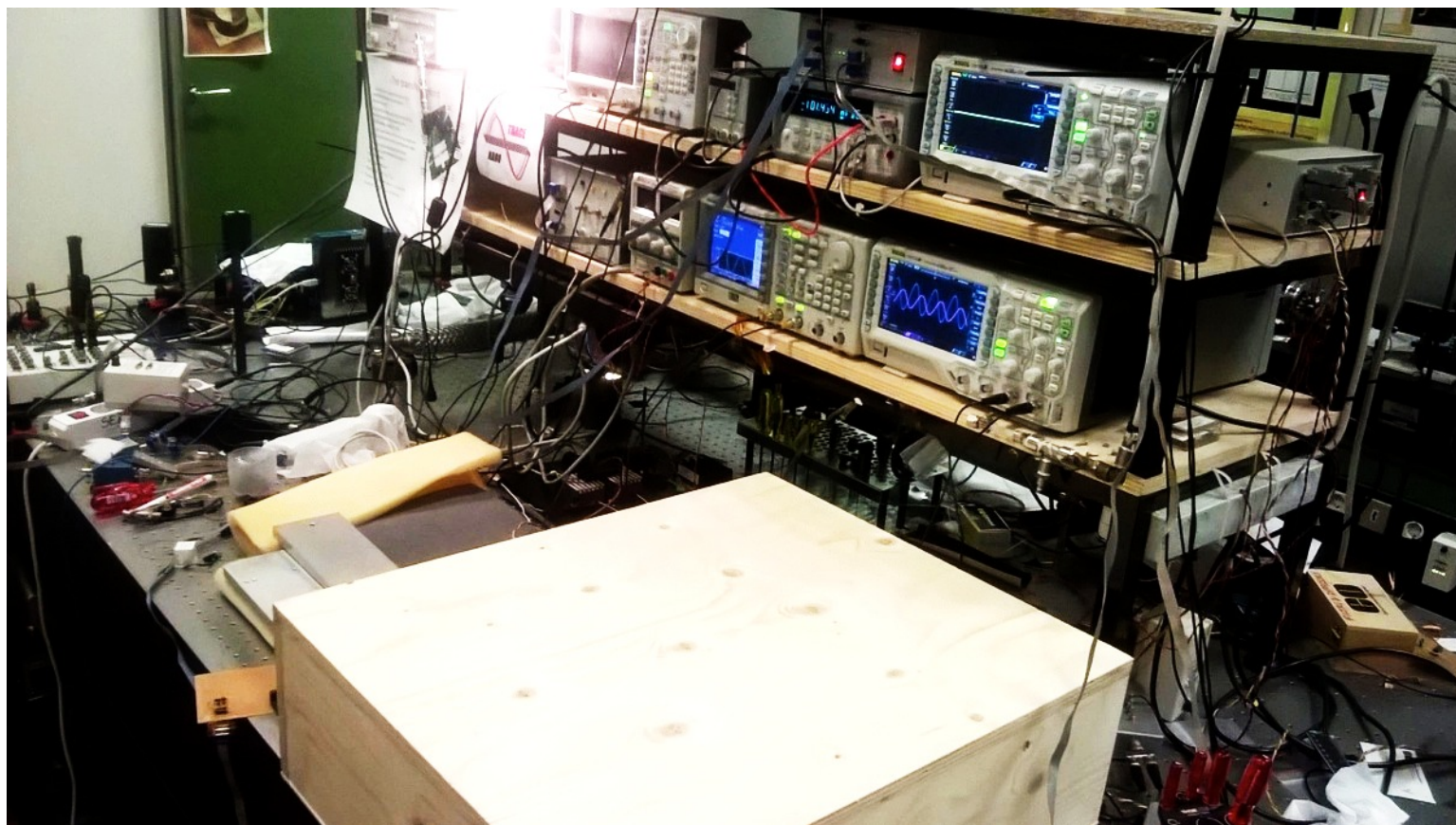
# PRA resolution/noise test

**10 pm p.p.** =  $10^{-7}$  of full range (about 10  $\mu\text{V}$  p.p. to the piezo)

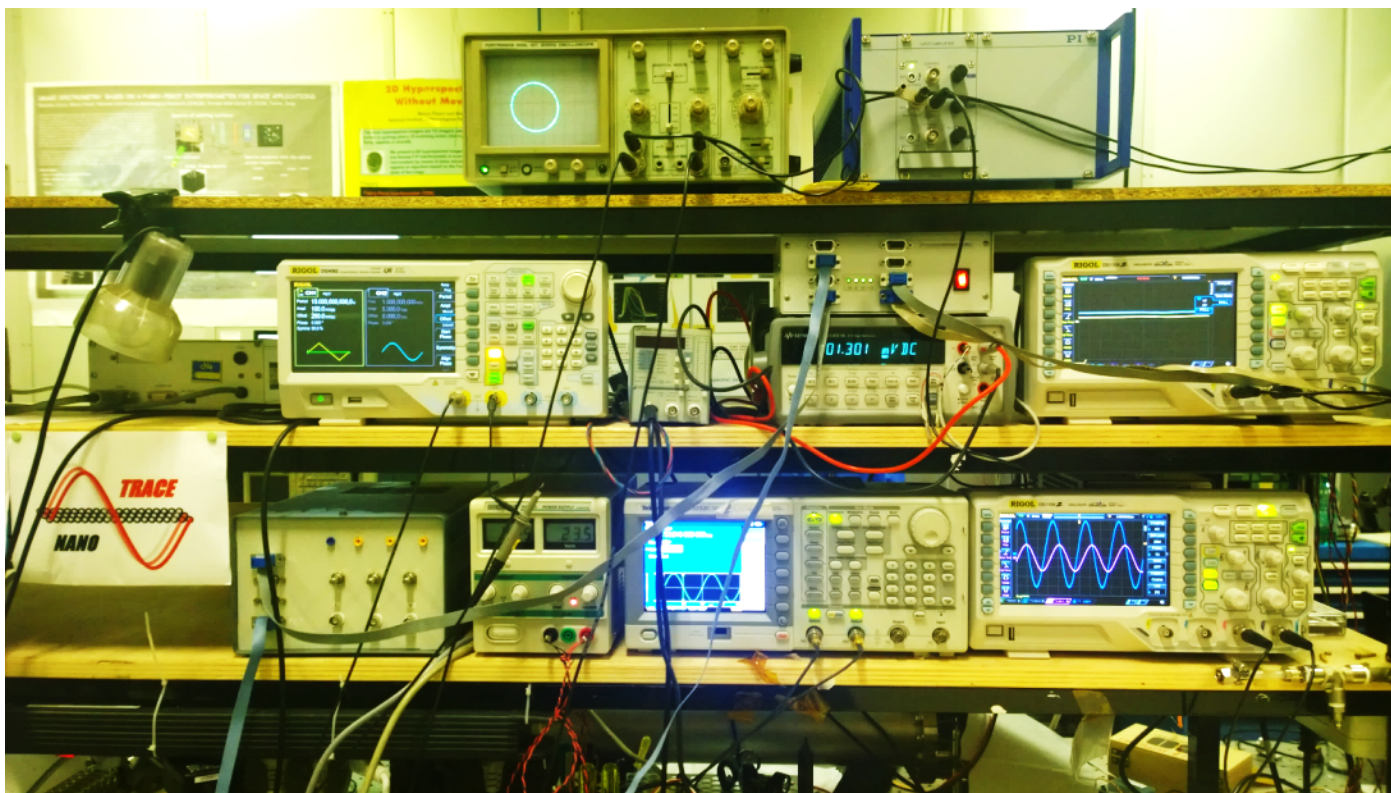


# LIG vs PRA

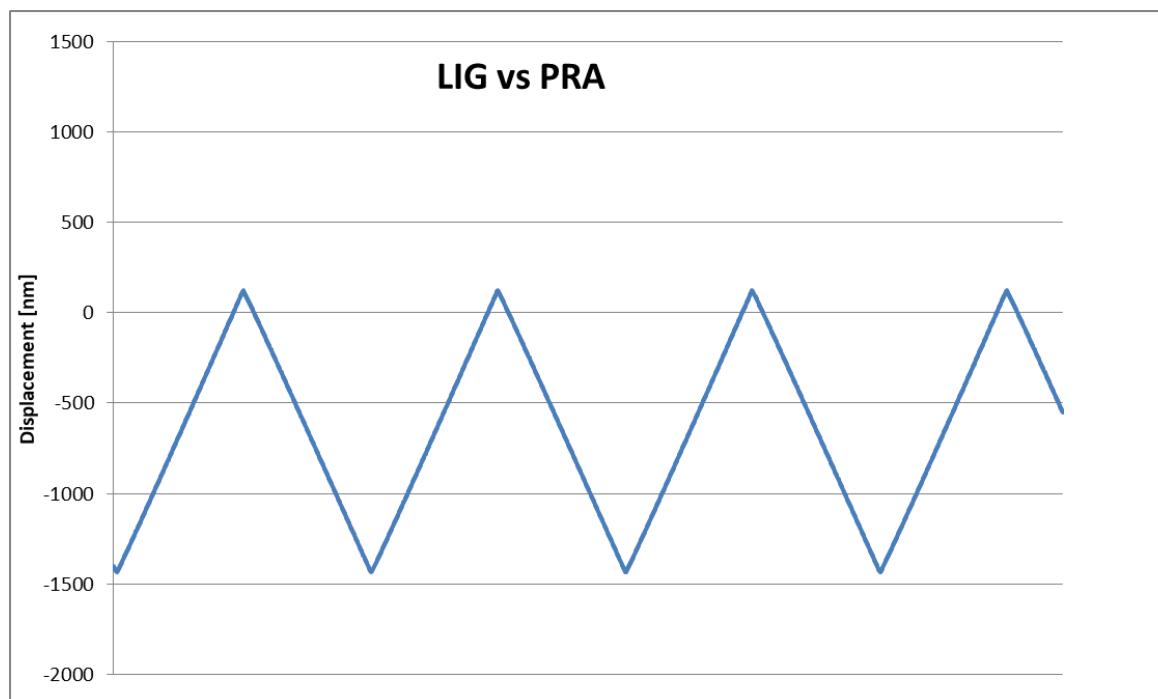




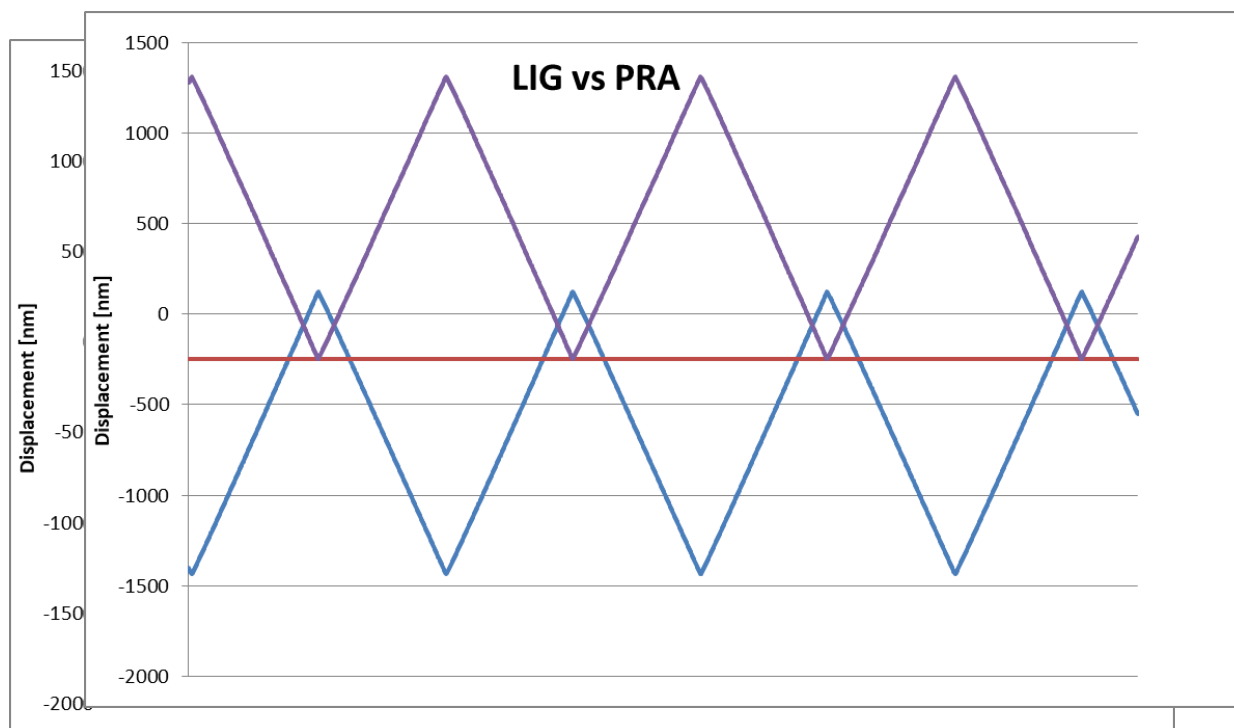
# LIG vs PRA



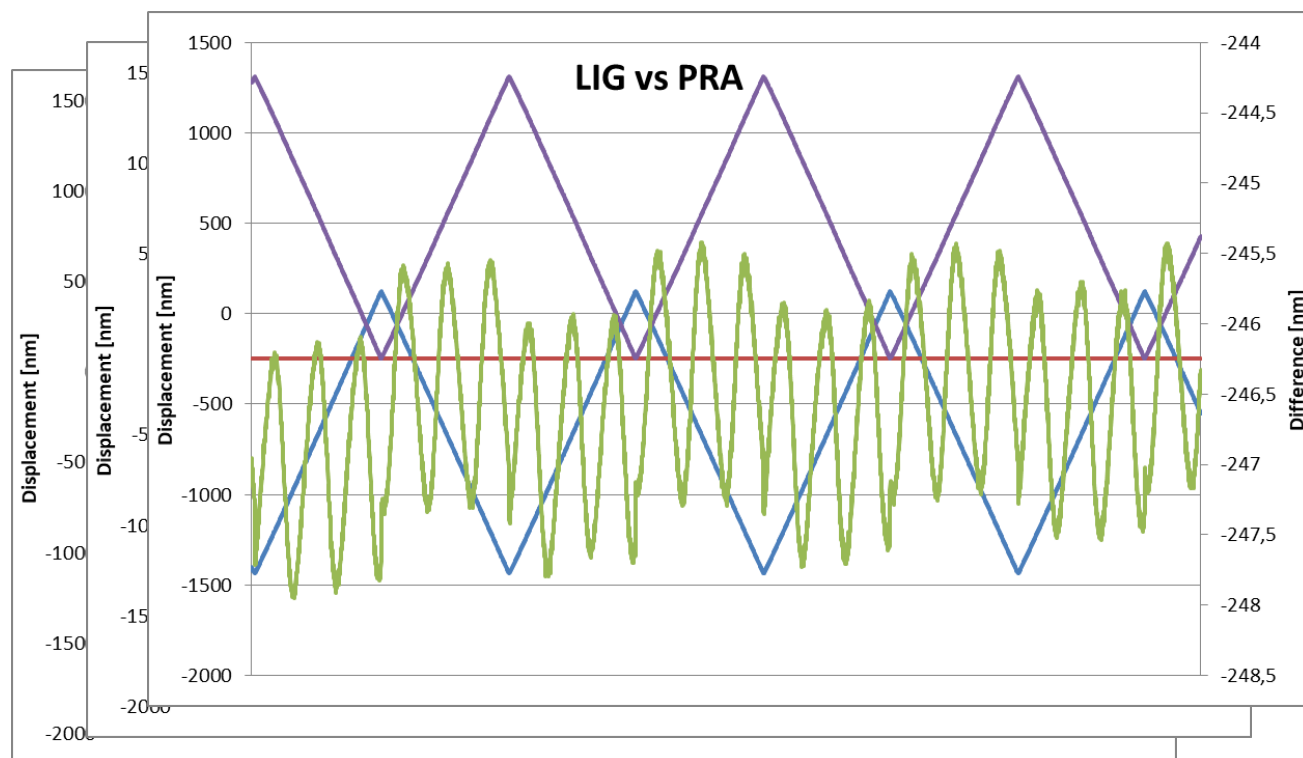
# LIG linearity test



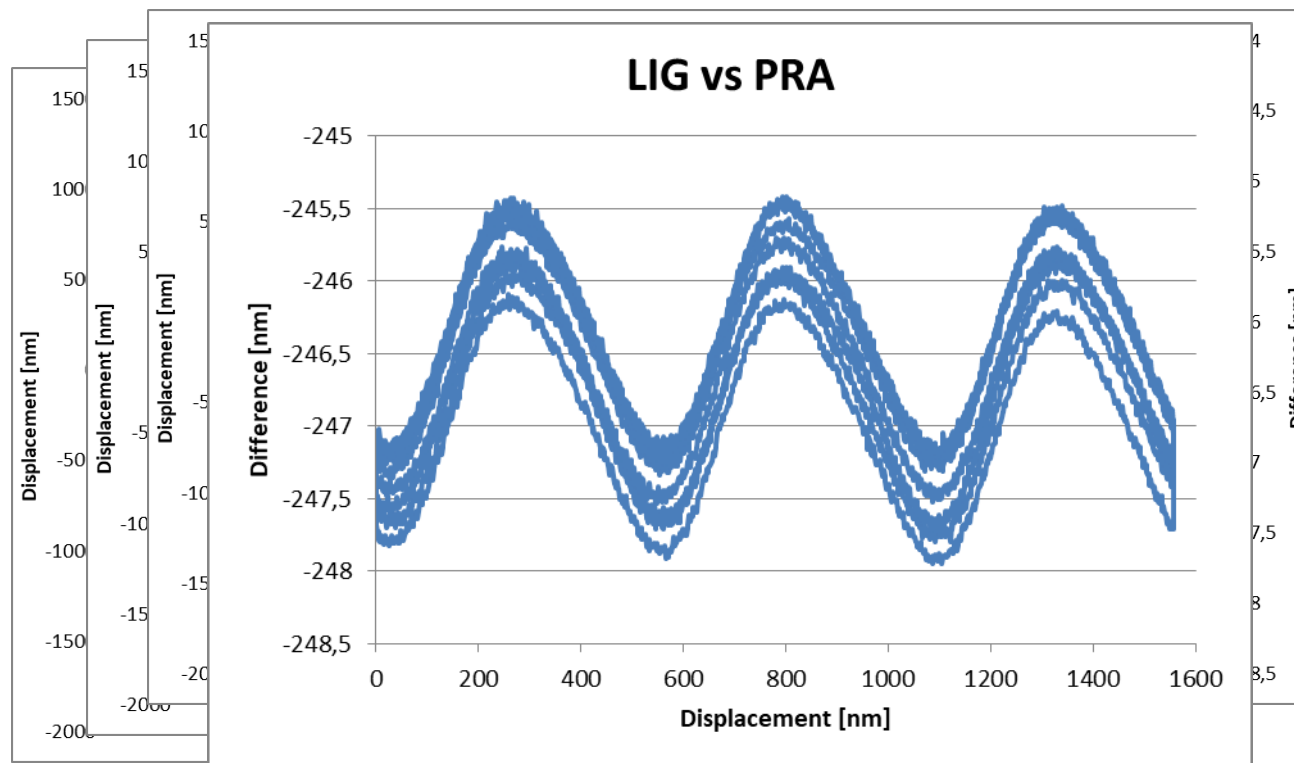
# LIG linearity test



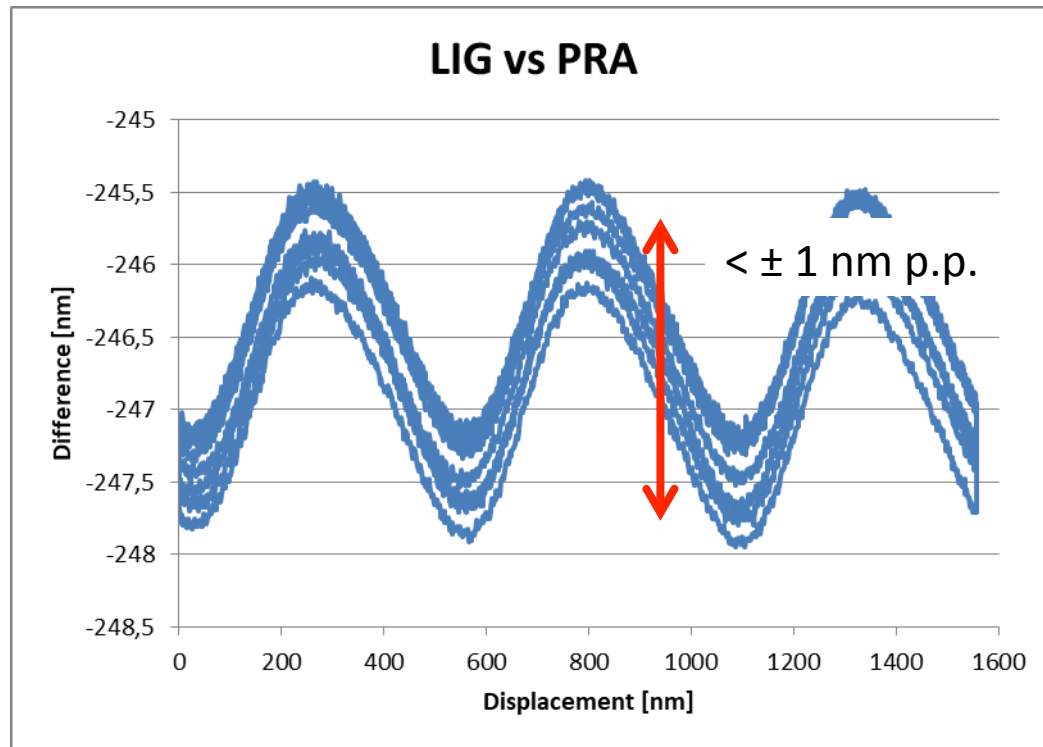
# LIG linearity test



# LIG linearity test



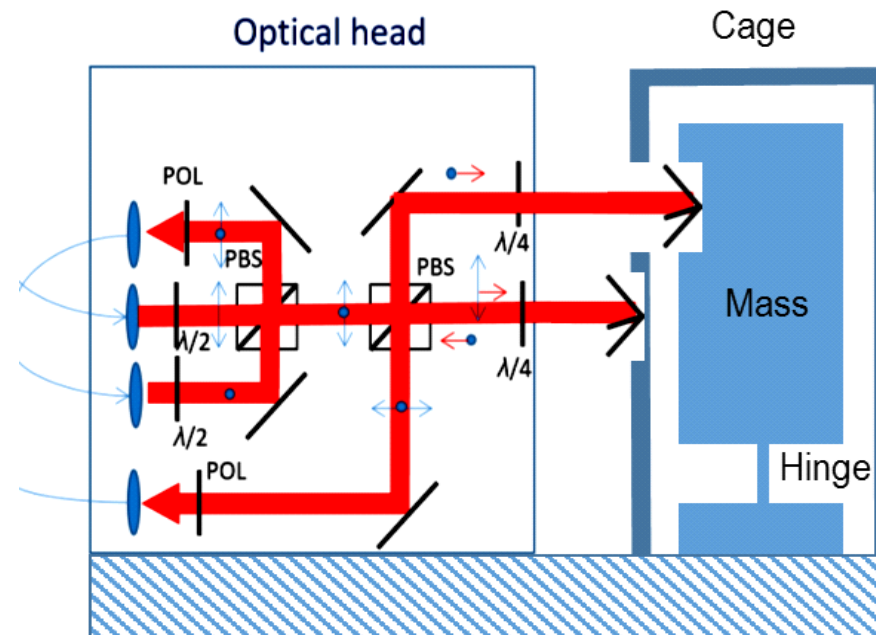
# Effect of non-linearity



- 1 nm error over 1  $\mu\text{m}$  wavelength  $\rightarrow$  max sensitivity error of 0.1% (e.g. 10 fm over 10 pm)
- This error could be further reduced by using better polarizing optics
- Furthermore, the cyclic error is a systematic behaviour of the interferometer that can be characterized and cancelled by post processing.

Next step

LIG-A (Laser Interferometry Gauge & Accelerometer):  
Integration of the interferometer in the accelerometer



# Conclusions

We have realized a simple and compact interferometer based on COTS components that can be used to replace capacitive sensors in accelerometers readout

The prototype has demonstrated picometer level resolution and nanometer level non-linearities over  $\mu\text{m}$  wavelength.

Next step is the realization of a more compact optical head which will be embedded in an existing spring-mass accelerometer